Visualization

CS 347
Michael Bernstein

Last time

Design principles provide strong guides for content creation tools: (1) identify design principles in expert output based on cognition/perception, and (2) instantiate them into algorithms to aid content creators, and (3) evaluate principles through user studies

Approach generalizes across a wide range of categories, ranging from digital illustration to audio, video, instructions and exploded views

Software and Tools

Unit 4

human-centered Al tools and toolkits content creation

Cognition Unit 5

cognitive models visualization (and don't forget the design cognition that we already covered)

Today

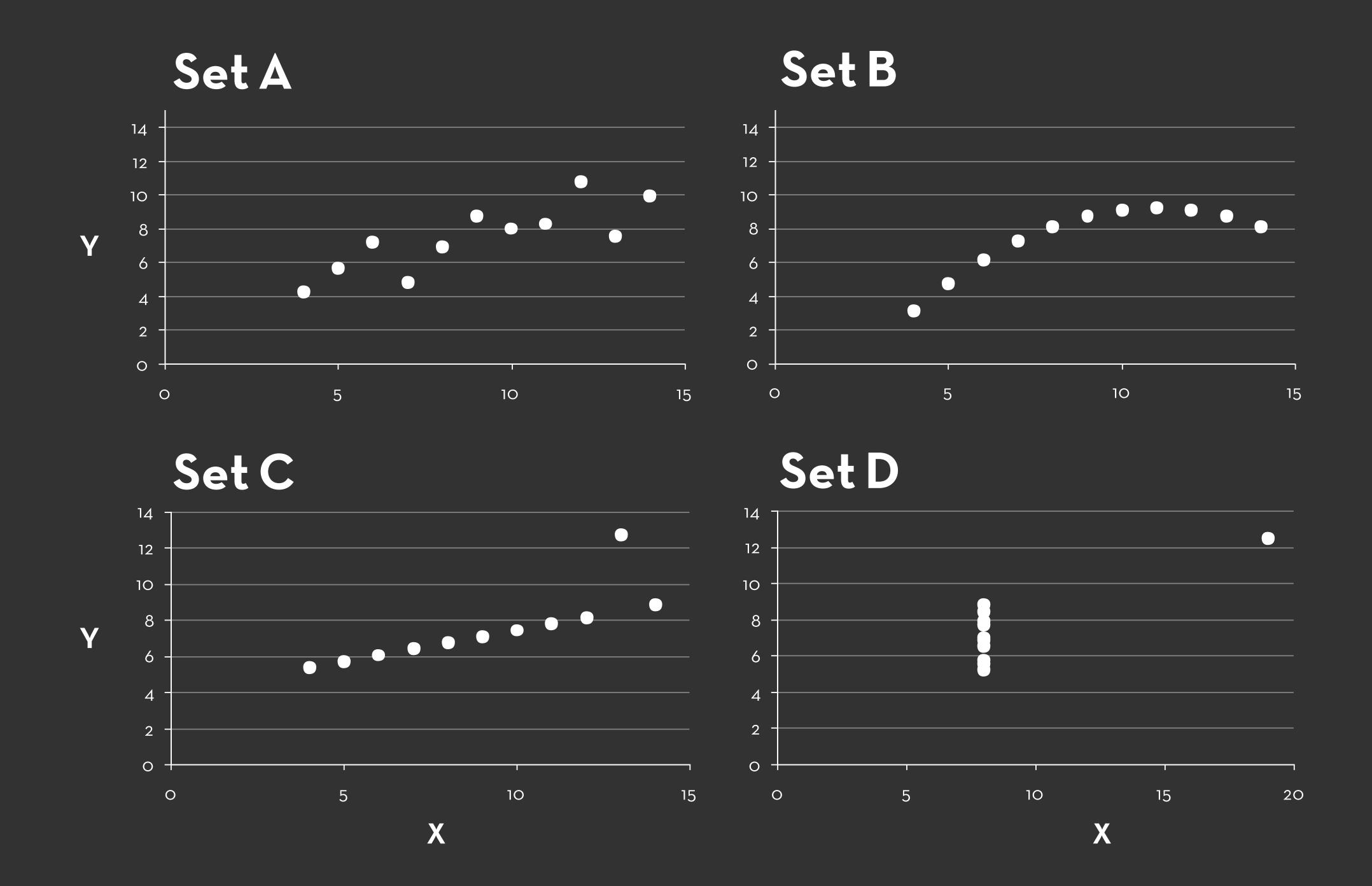
Data, marks, visual attributes and encodings

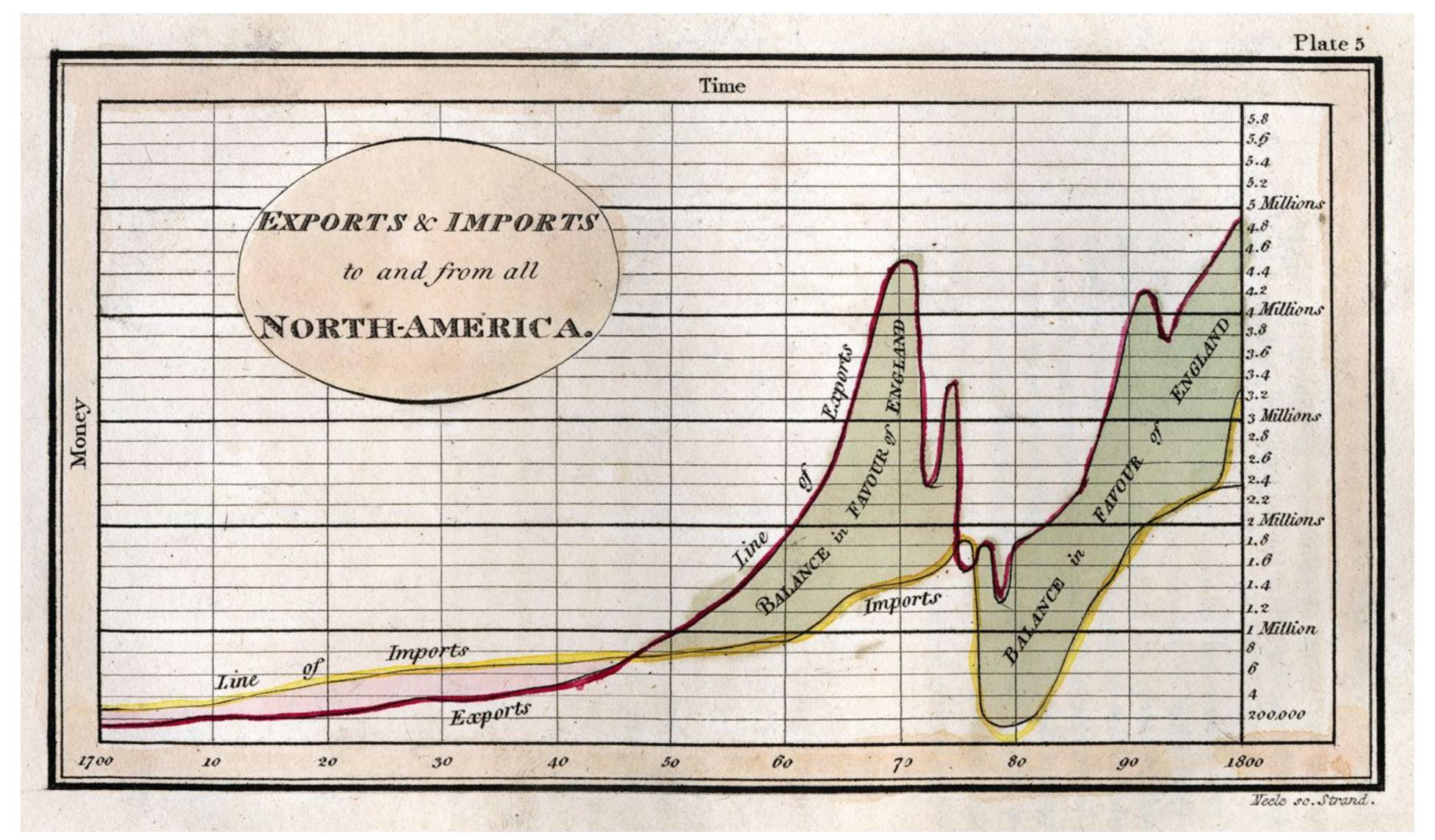
Graphical perception

Frontiers of visualization research

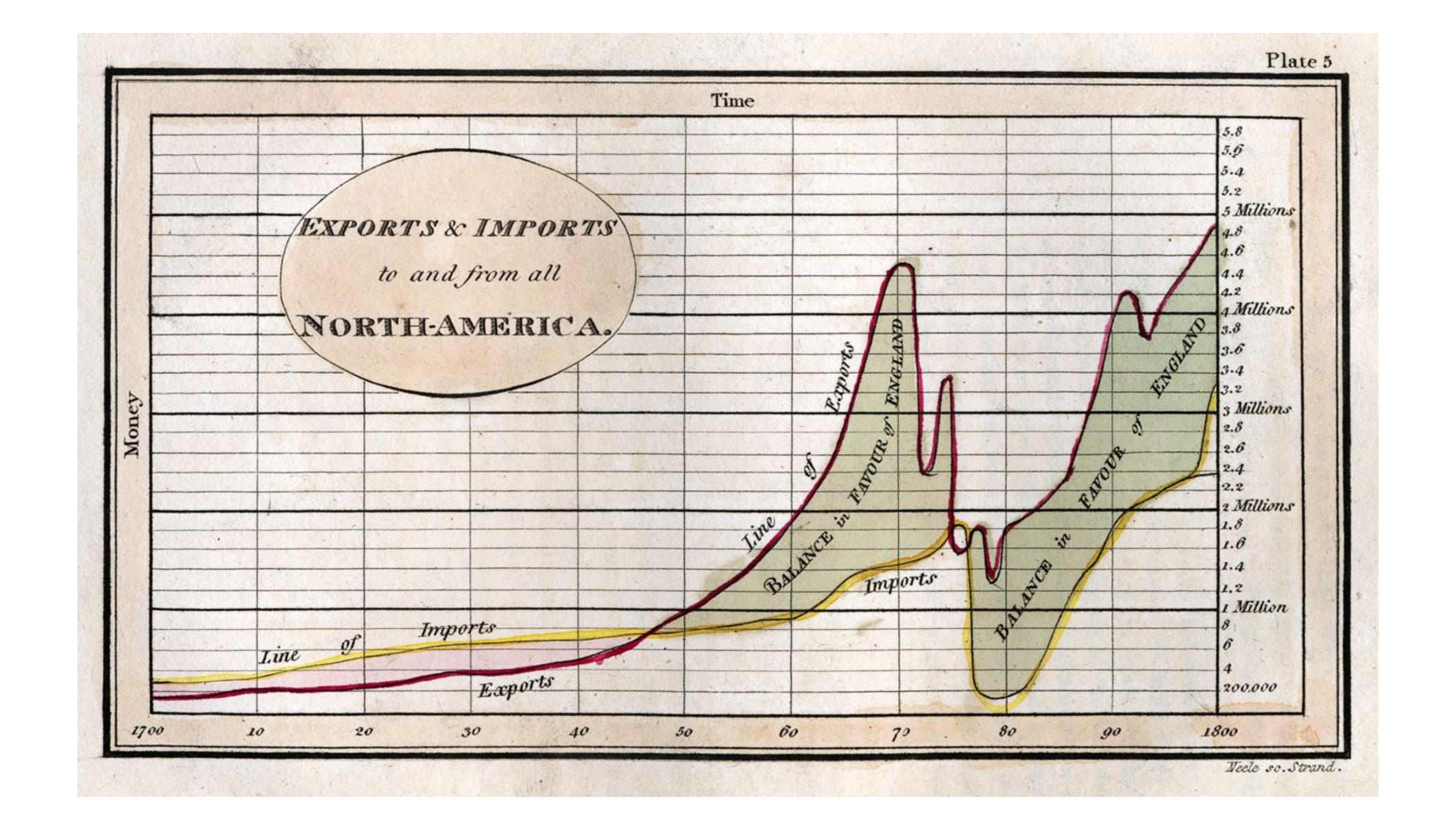
Anscombe's Quartet [Anscombe 1973]

Set A		Se	Set B		Set C		t D		
	Χ	Υ	X	Υ	X	Υ	X	Υ	Summary Statistics
	10	8.04	10	9.14	10	7.46	8	6.58	$u_X = 9.0 \sigma_X = 3.317$
	8	6.95	8	8.14	8	6.77	8	5.76	$u_Y = 7.5 \sigma_Y = 2.03$
	13	7.58	13	8.74	13	12.74	8	7.71	
	9	8.81	9	8.77	9	7.11	8	8.84	Linear Regression
	11	8.33	11	9.26	11	7.81	8	8.47	Y = 3 + 0.5 X
	14	9.96	14	8.1	14	8.84	8	7.04	$R^2 = 0.67$
	6	7.24	6	6.13	6	6.08	8	5.25	
	4	4.26	4	3.1	4	5.39	19	12.5	
	12	10.84	12	9.11	12	8.15	8	5.56	
	7	4.82	7	7.26	7	6.42	8	7.91	
	5	5.68	5	4.74	5	5.73	8	6.89	6

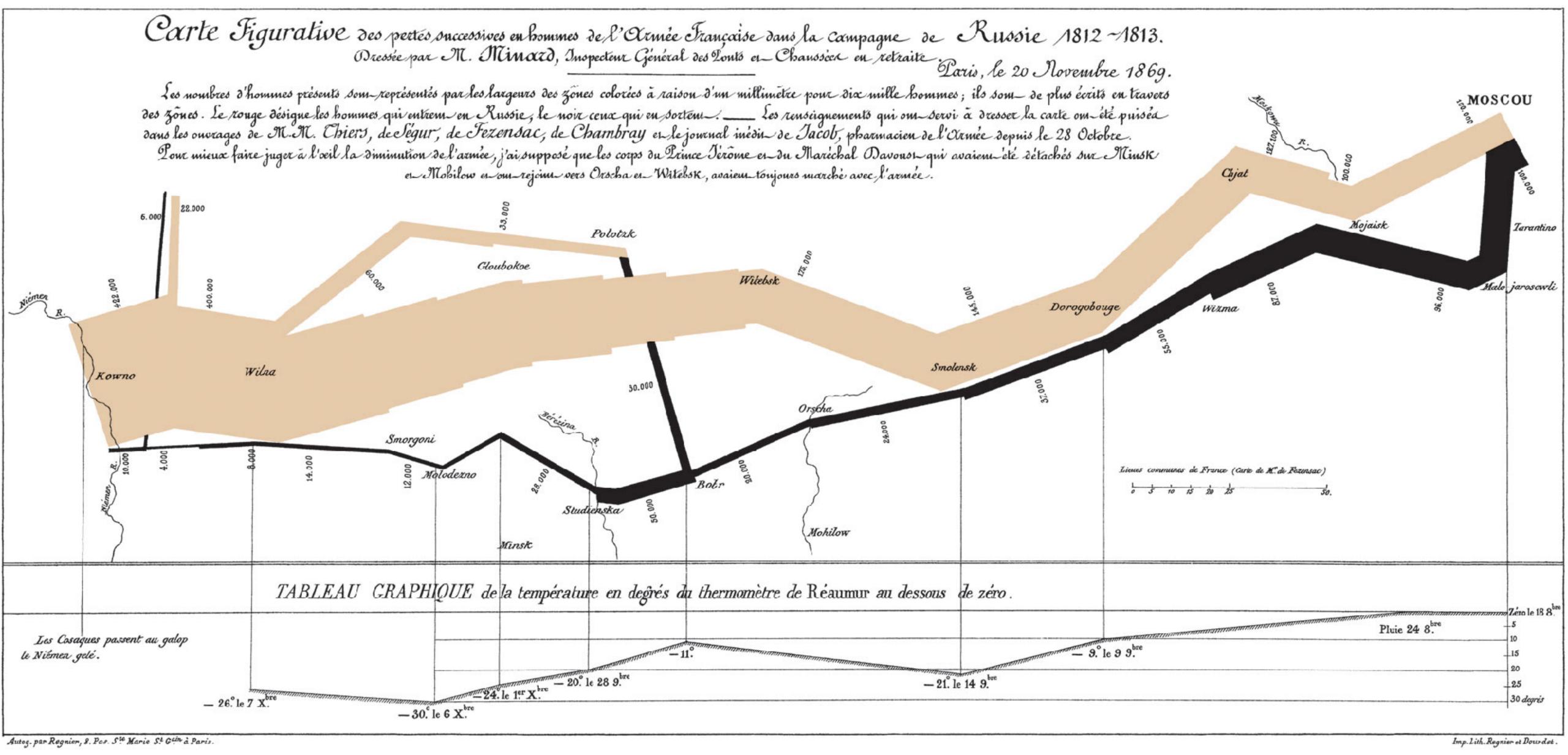




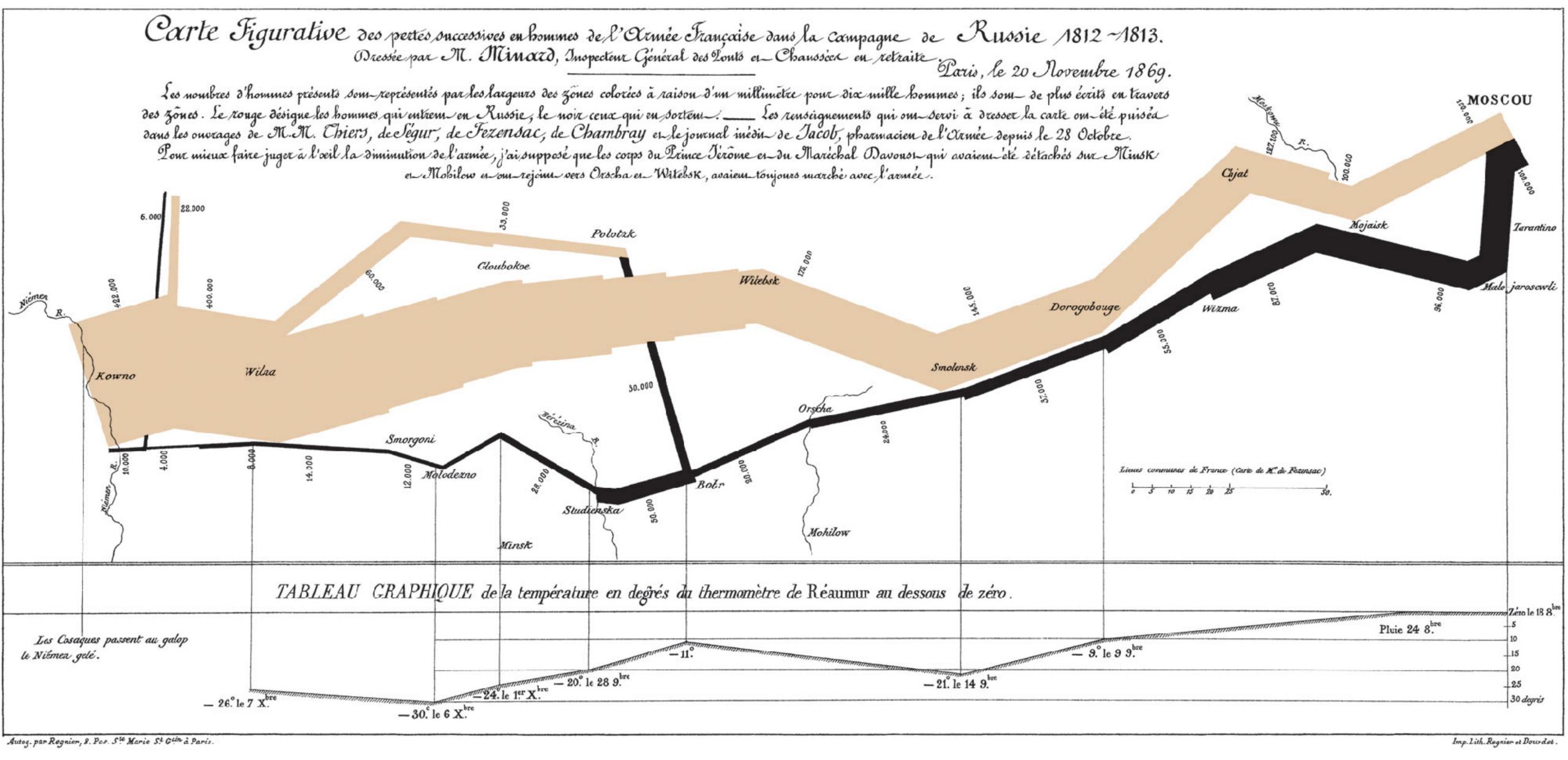
Exports and Imports to and from all North America [Playfair 1786] Important information: differences between exports and imports



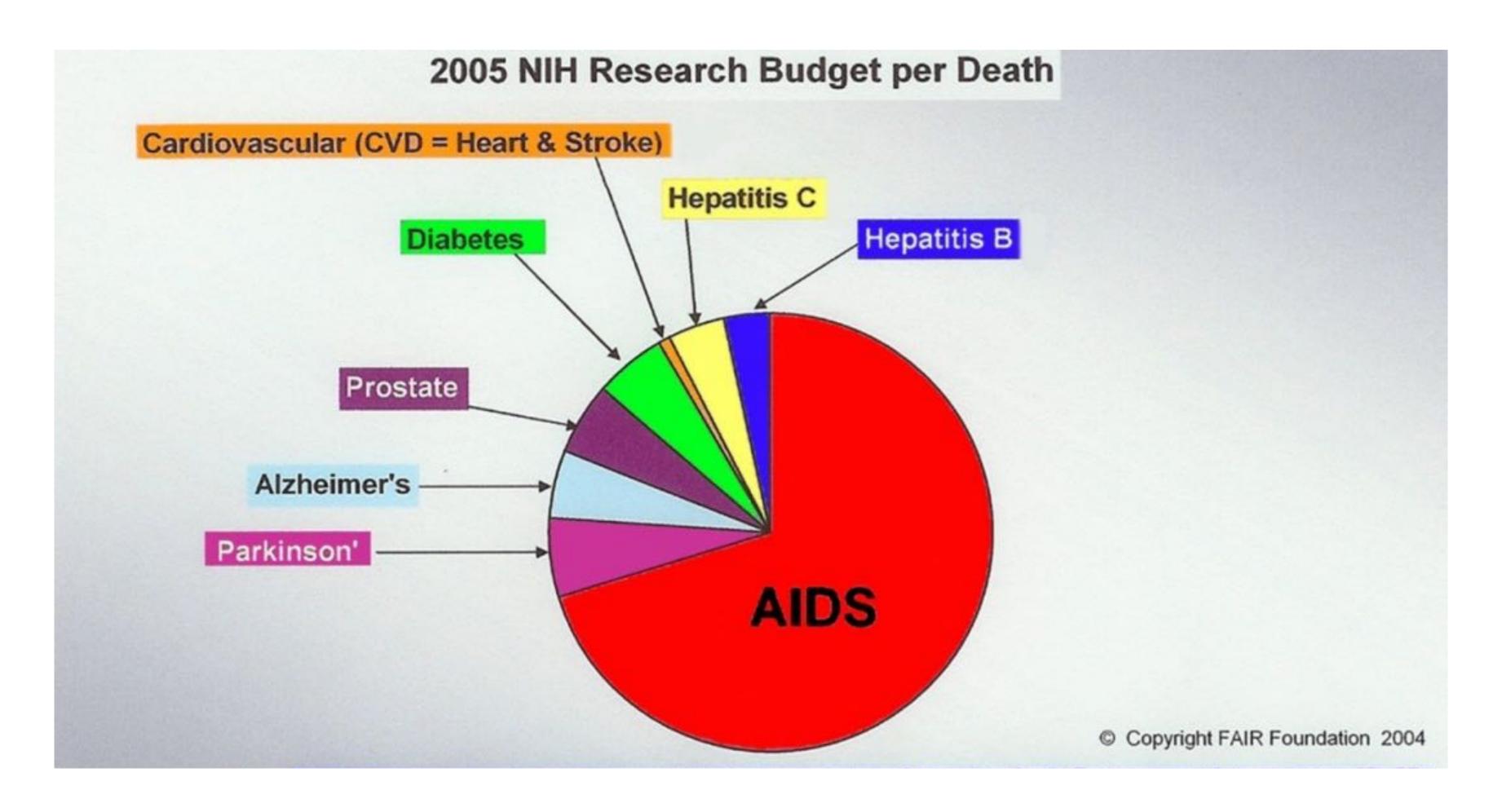
Design principle: shade areas between lines to highlight differences



Charles Minard [1869]

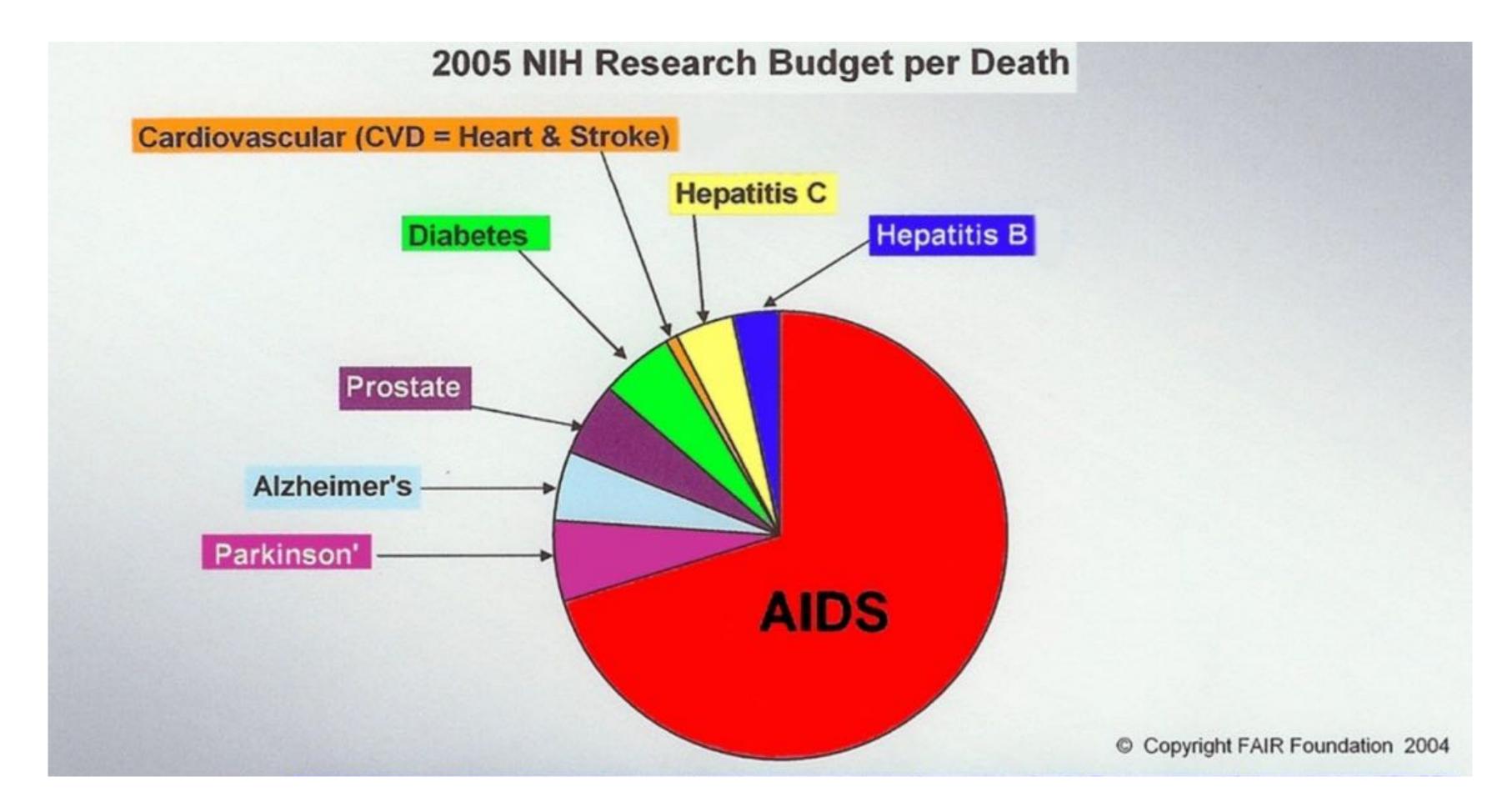


Important information: army size decreasing as Napoleon marches Design principle: use flow diagram width to convey the drop in army size



Estimated 2005 NIH Research Budget per Death [FAIR Foundation 04]

User's task: Understand proportion of budget allocated to each disease, and compare proportion of budget allocated to each disease



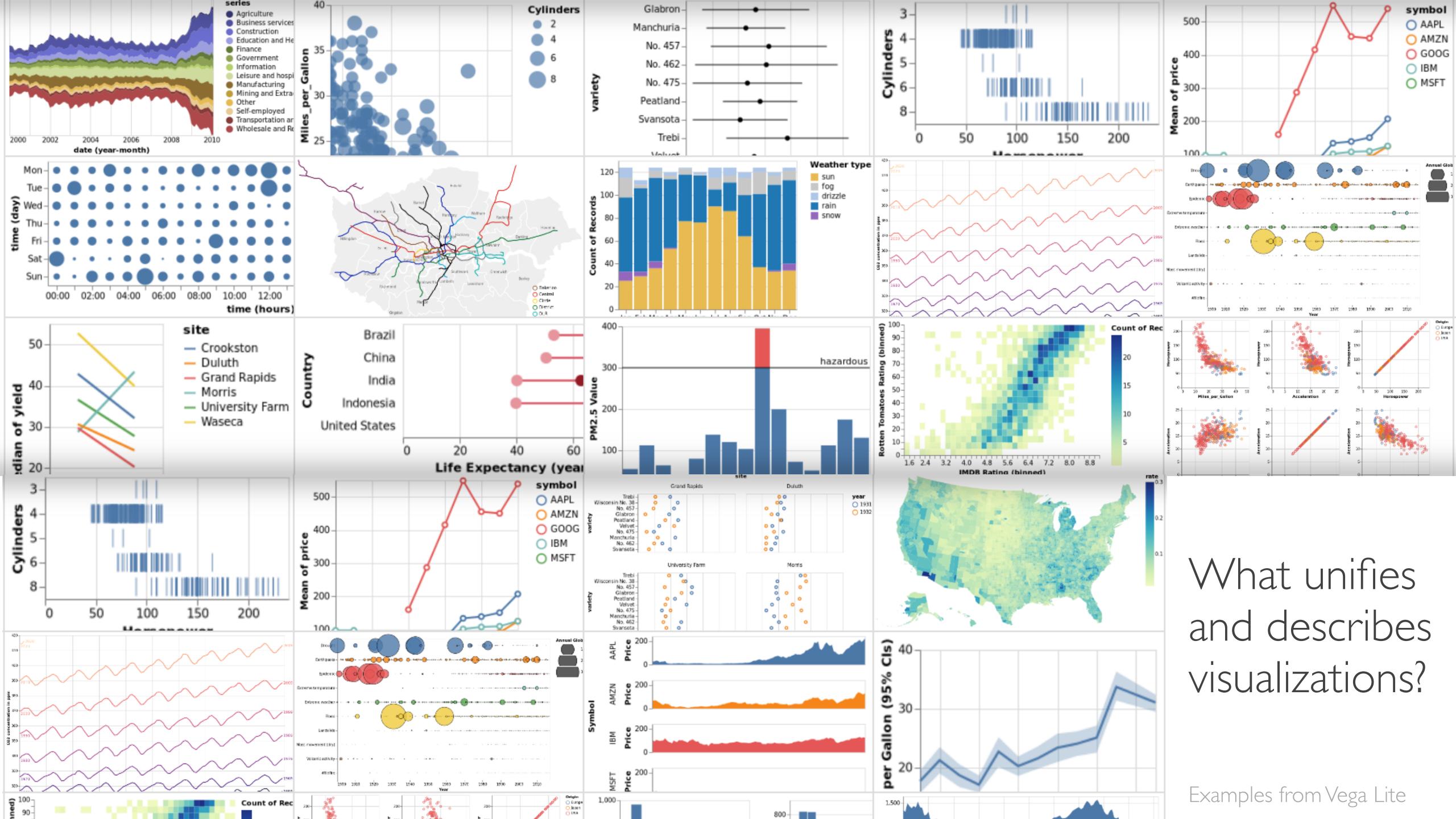
Representation: pie chart to emphasizes part-to-whole relationship

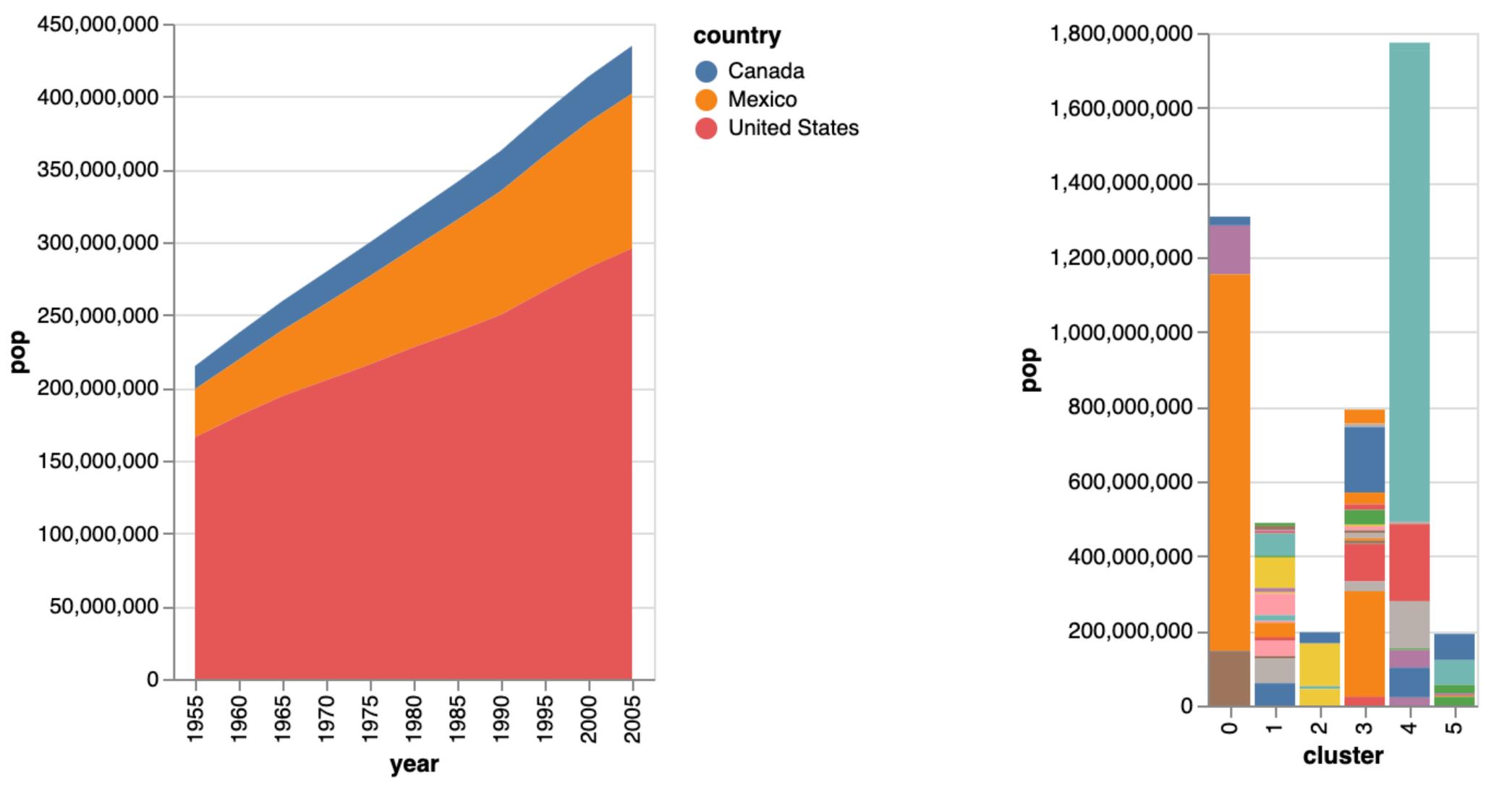
But, a failure: doesn't easily comparison between diseases by comparing pie slices (angles or areas)

What is visualization?

- "Transformation of the symbolic into the geometric" [McCormick et al. 1987]
- "...finding the artificial memory that best supports our natural means of perception." [Bertin 1967]
- "The use of computer-generated, interactive, visual representations of data to amplify cognition." [Card, Mackinlay, and Shneiderman 1999]

Data, marks, visual attributes and encodings





What precisely makes these visualizations—of the same dataset—different? [Heer 2021]

Anatomy of a visualization

Visualizations comprise a few main elements:

Data: the information to be visualized

Marks: geometric primitives, e.g., points, lines, areas

Visual attributes: transformations on the marks, e.g., size

Encodings: functions that map from data onto marks and visual variables

Let's introduce each of these in turn.

Data: types of data [Stevens 1946]

Nominal: category labels, no inherent ordering

e.g., apples, oranges operations: =, ≠

Ordinal: ordered, but no notion of "distance"

e.g., freshman, sophomore, junior, senior | operations: =, \neq , <, >, \leq , \geq

Quantitative: can be compared via differences or ratios

intervals, e.g., dates, lat/lon | operations: =, \neq , <, >, \le , \ge , =

ratios, e.g., length, mass, temperature | operations: =, \neq , <, >, \leq , \geq , -, \div

Same info, different type

Floating point numbers: 32.5, 54.0, -17.3

plus

Conceptual model: temperature

equals

Different possible data types:

Nominal: burned or not burned

Ordinal: cold, warm, hot

Quantitative: °F

U.S. Census Data

People Count: # of people in group

Year: 1850 – 2000 (every decade)

Age: 0 - 90 +

Sex: Male, Female (Census classification)

Marital Status: Single, Married, Divorced, ...

Α	В	С	D	E
year	age	marst	sex	people
1850	0	0	1	1483789
1850	0	0	2	1450376
1850	5	0	1	1411067
1850	5	0	2	1359668
1850	10	0	1	1260099
1850	10	0	2	1216114
1850	15	0	1	1077133
1850	15	0	2	1110619
1850	20	0	1	1017281
1850	20	0	2	1003841
1850	25	0	1	862547
1850	25	0	2	799482
1850	30	0	1	730638
1850	30	0	2	639636
1850	35	0	1	588487
1850	35	0	2	505012
1850	40	0	1	475911
1850	40	0	2	428185
1850	45	0	1	384211
1850	45	0	2	341254
1850	50	0	1	321343
1850	50	0	2	286580
1850	55	0	1	194080
1850	55	0	2	187208
1850	60	0	1	174976

Census

People Count: Quantitative

Year: Quantitative

Age: Quantitative

Sex: Nominal

Marital Status: Nominal

Α	В	С	D	E
year	age	marst	sex	people
1850	0	0	1	1483789
1850	0	0	2	1450376
1850	5	0	1	1411067
1850	5	0	2	1359668
1850	10	0	1	1260099
1850	10	0	2	1216114
1850	15	0	1	1077133
1850	15	0	2	1110619
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1850	40	0	1	475911
1850	40	0	2	428185
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1850	50	0	1	321343
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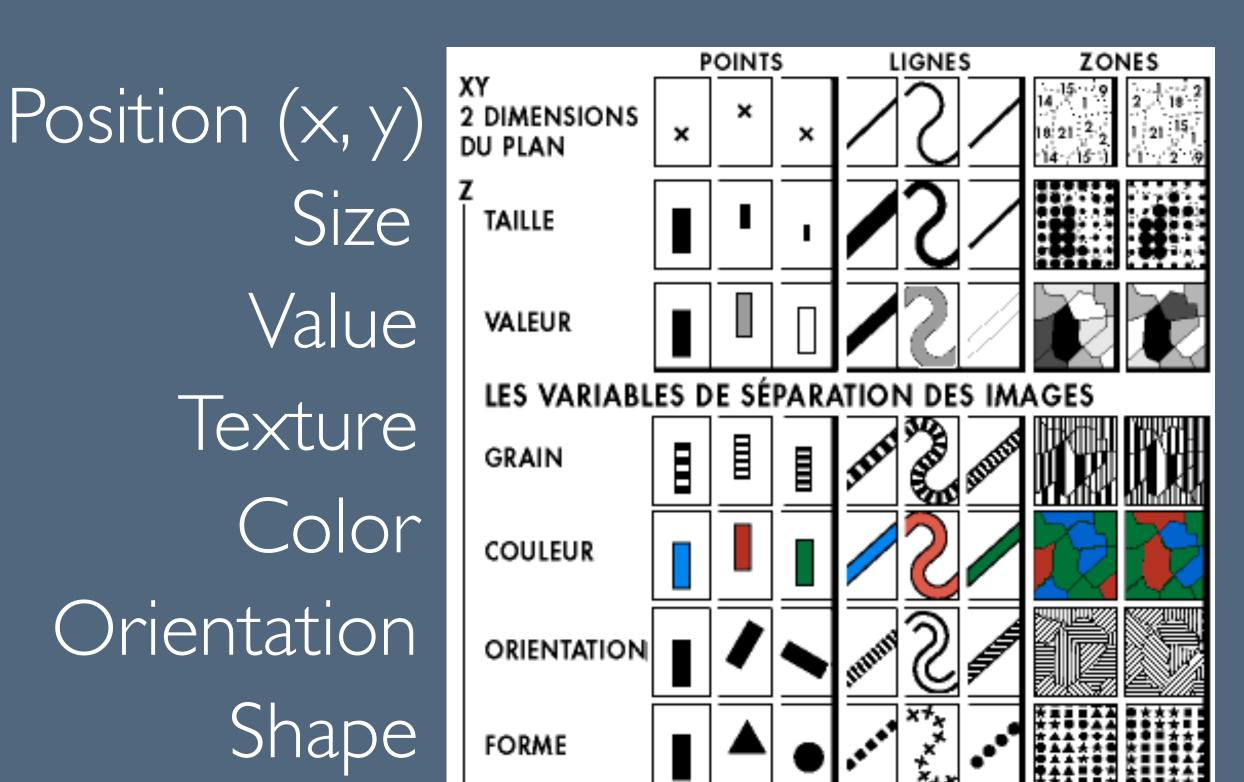
Marks and visual variables

[Bertin 1967]

Marks: geometric primitives

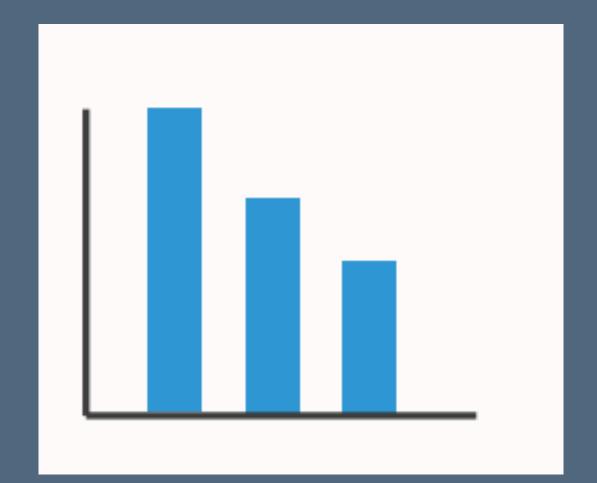
Visual attributes: control mark appearance





Encodings

A map from data to visual attributes of marks

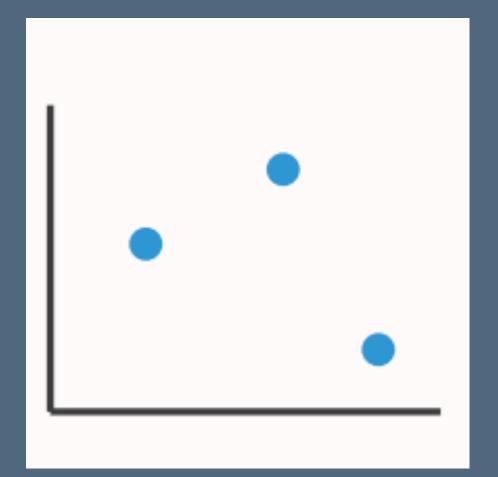


Mark: bar

county(nominal) → x

population(quant) →

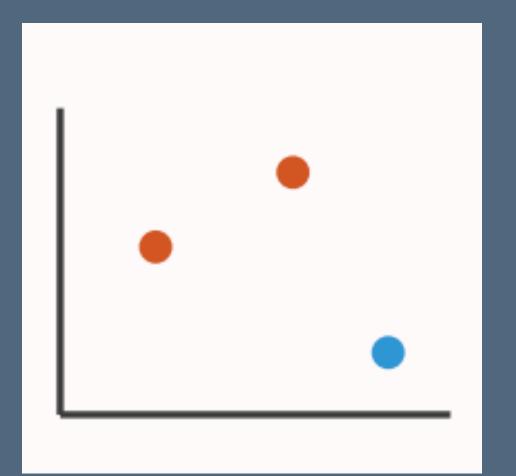
size or length



Mark: point

acreage(quant) → x

population(quant) → y



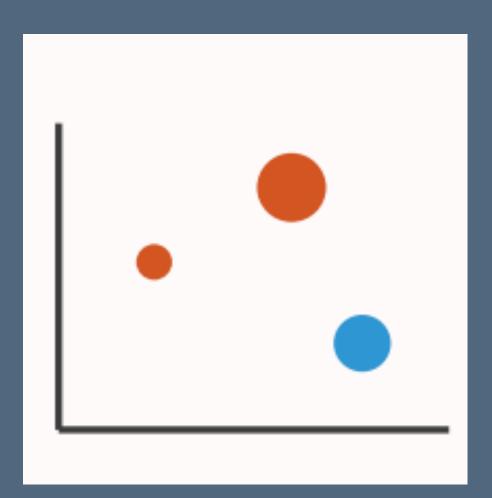
Mark: point

acreage(quant) → x

population(quant) → y

county(nominal) →

color



Mark: point

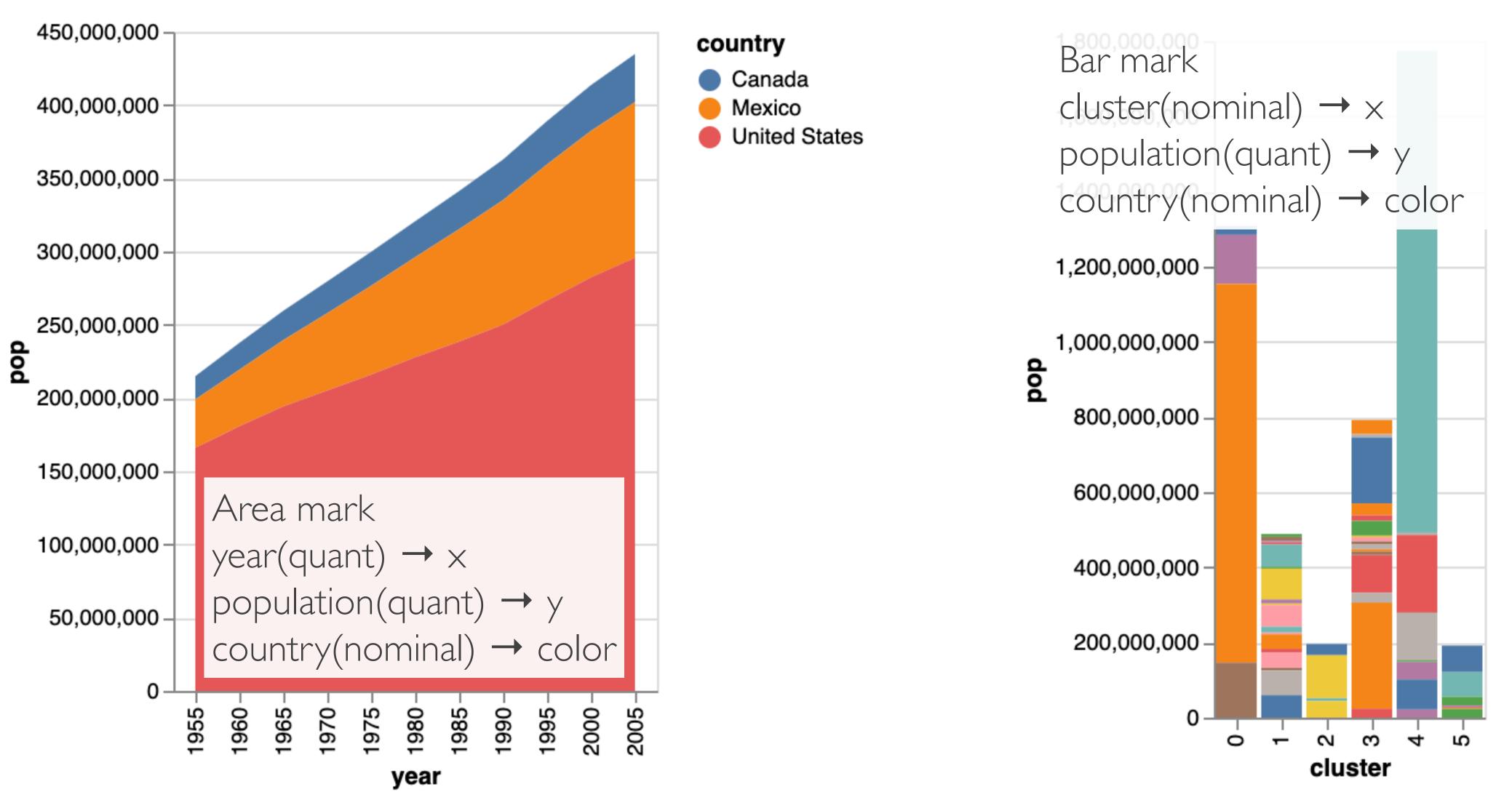
acreage(quant) → x

population(quant) → y

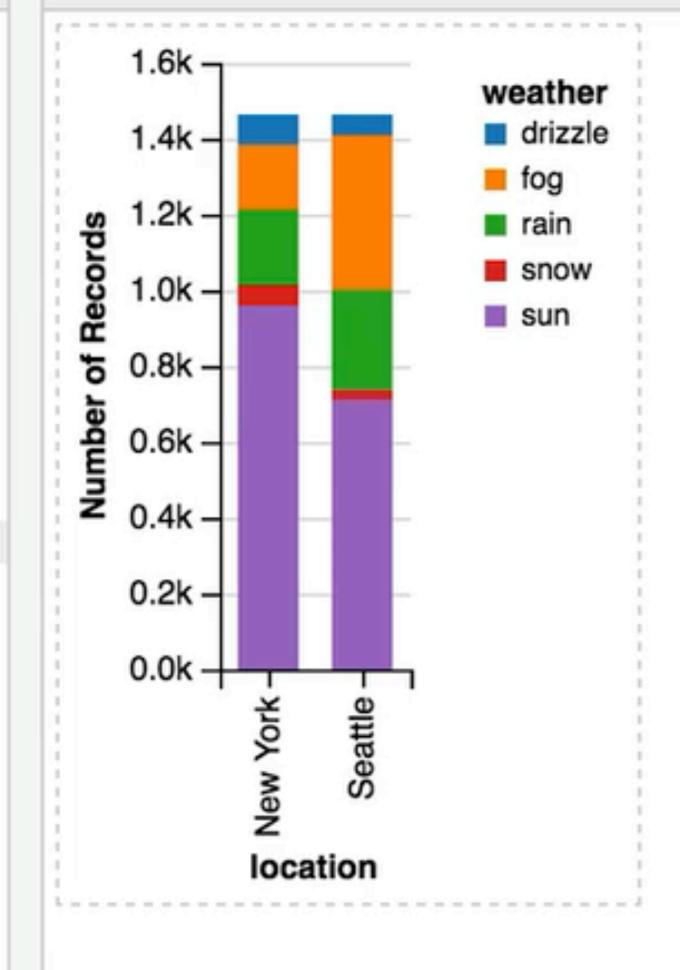
county(nominal) → color

avg_income(quant) → size

"Best" encoding based on perceptual effectiveness of visual attribute for data type



What precisely makes these visualizations—of the same dataset—different? [Heer 2021]



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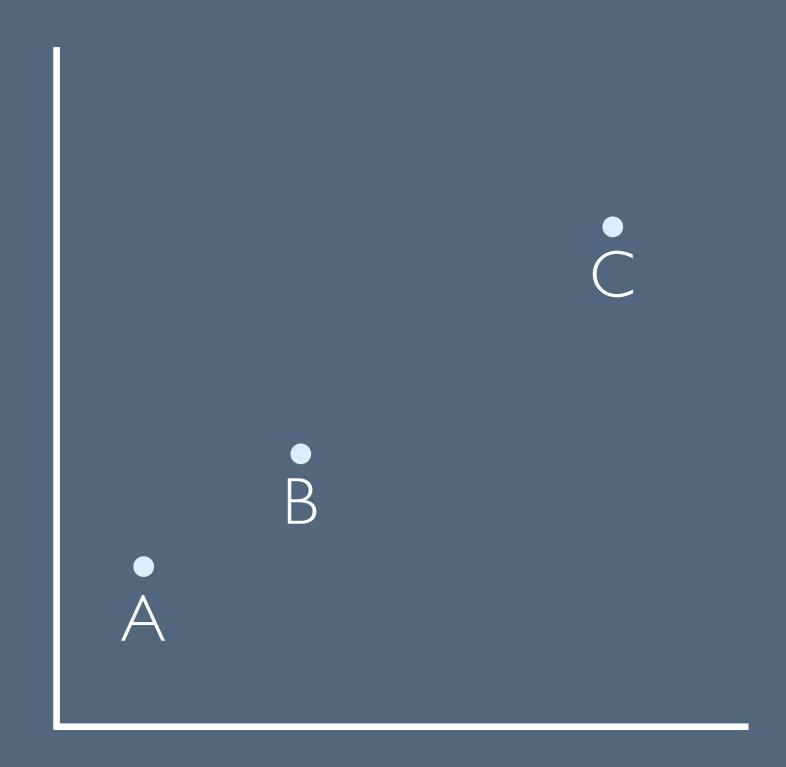
[Satyanarayan et al. 2016]

Graphical perception

How we look at graphs



Position



We immediately notice that:

A, B, C are distinguishable

Points are collinear. B is between A and C

BC is twice as long as AB

Position encodes quantitative data well

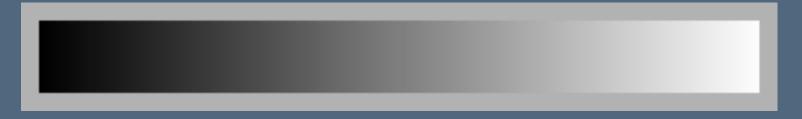
Color

Value or gray level is perceived as ordered

So, it encodes ordinal data well



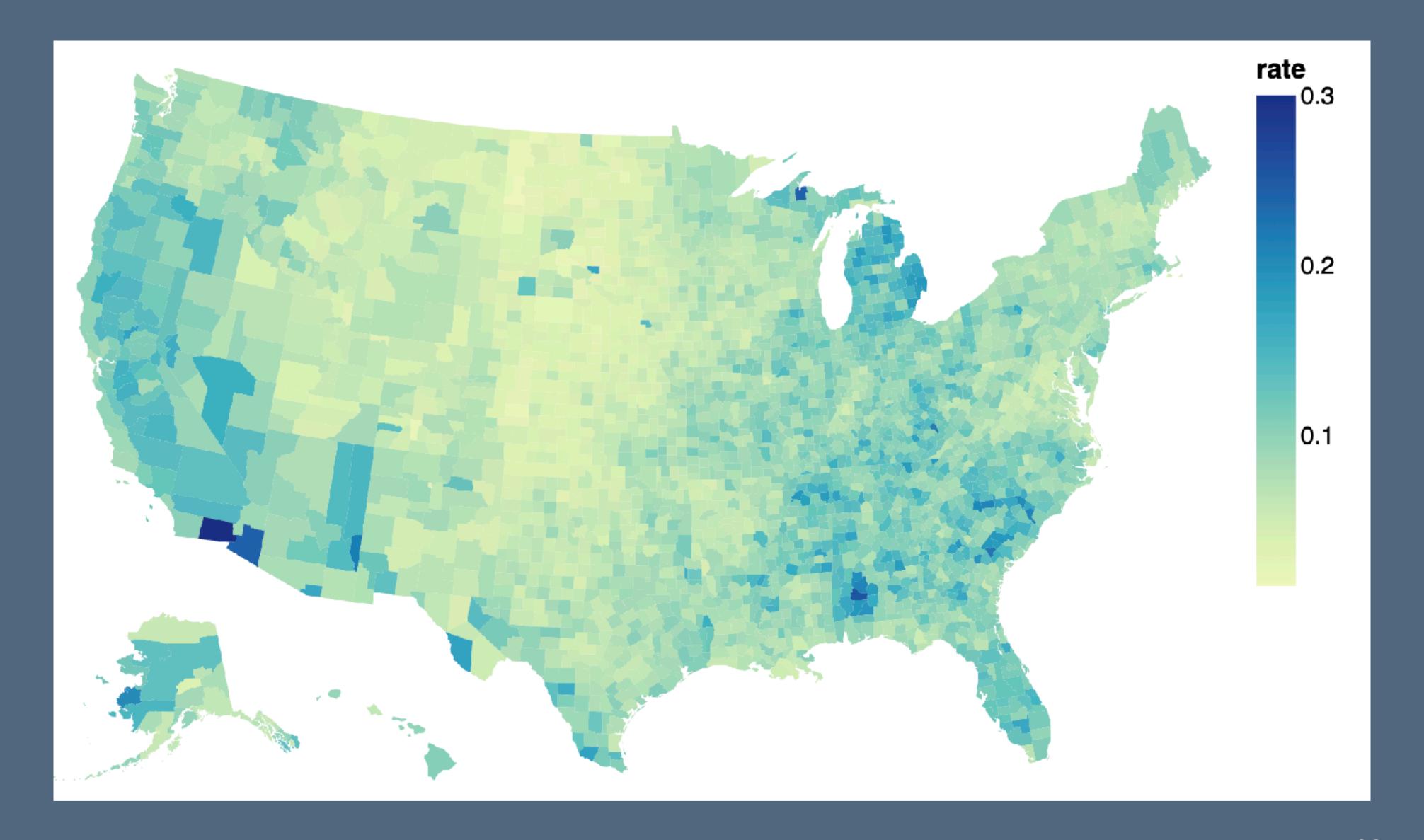
But, fine differences hard to perceive, so encodes quantitative data less well



Hue is typically perceived as unordered

So, hue encodes nominal data well





We can perceive which areas have higher rates, but it takes effort to understand **how much** higher the rates are (2x? 3x?)

Bertin's "Levels of Organization"

[Bertin 1967]

Ranking of visual variables in terms of how well they can represent different kinds of data: e.g., position and size are good for all data types

Position	Nominal	Ordinal	Quantitative
Size	Nominal	Ordinal	Quantitative
Value	Nominal	Ordinal	(quantitative)
Texture	Nominal	(ordinal)	
Color	Nominal		
Orientation	Nominal		
Shape	Nominal		

Which is brighter? With only a quick visual judgment:

Which is brighter? With only a quick visual judgment:

Which is brighter? With only a quick visual judgment:

Which is brighter? With only a quick visual judgment:

(128, 128, 128) (130, 130, 130)





Re-encoding the same comparison as length rather than area:

Re-encoding the same comparison as length rather than area:

Re-encoding the same comparison as length rather than area:

Re-encoding the same comparison as length rather than area:

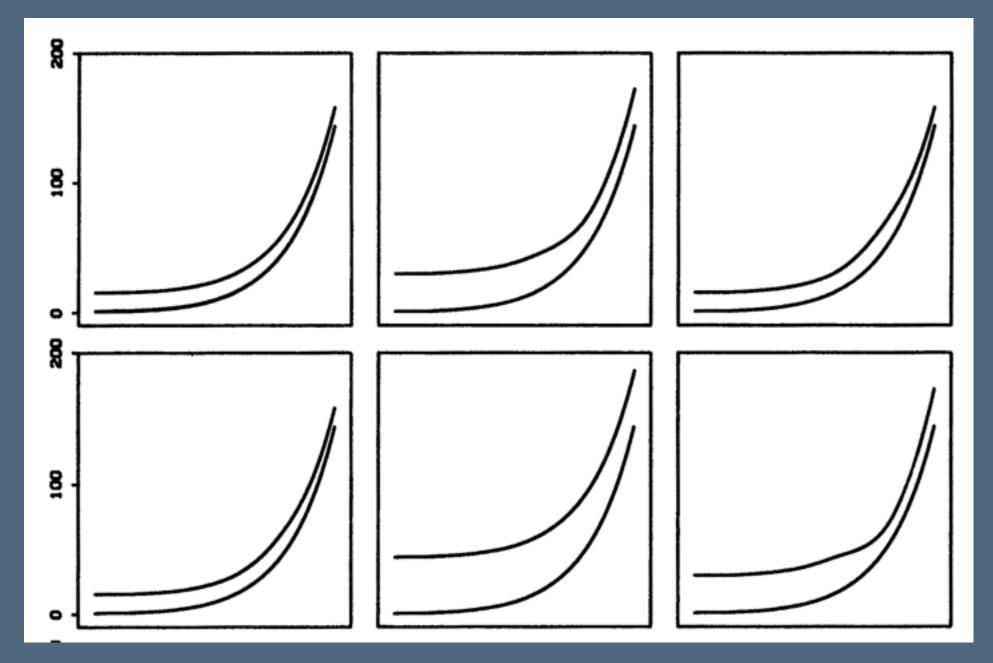
1000 pixels

1392 pixels

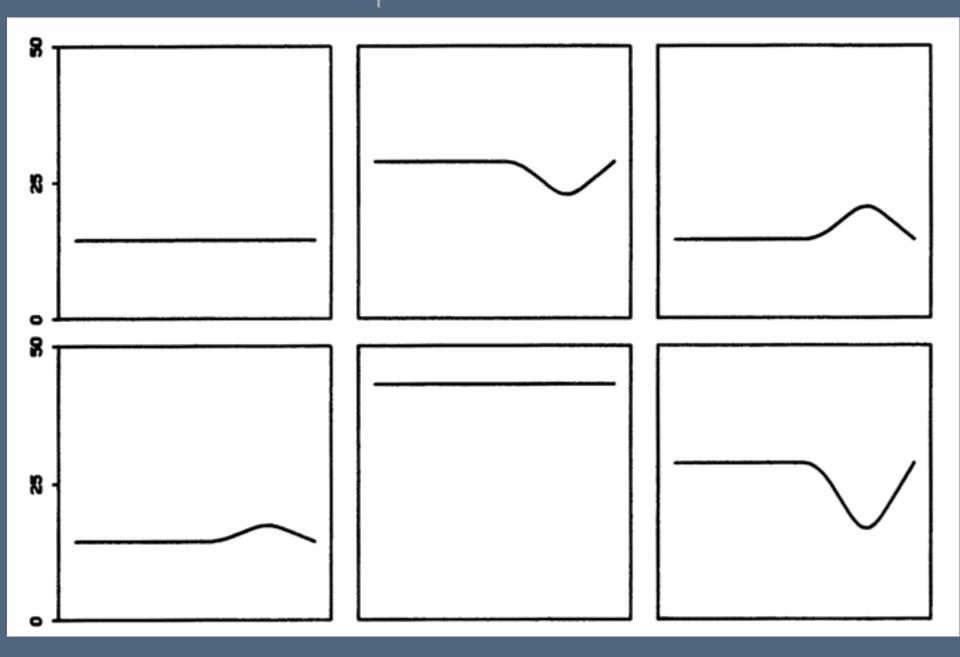
We are poor at perceiving (some) differences [Cleveland and McGill 1984]

Classic result: experimental tests of the relationship between encodings and the accuracy of the differences that we perceive from those encodings

What are the distances between these lines?

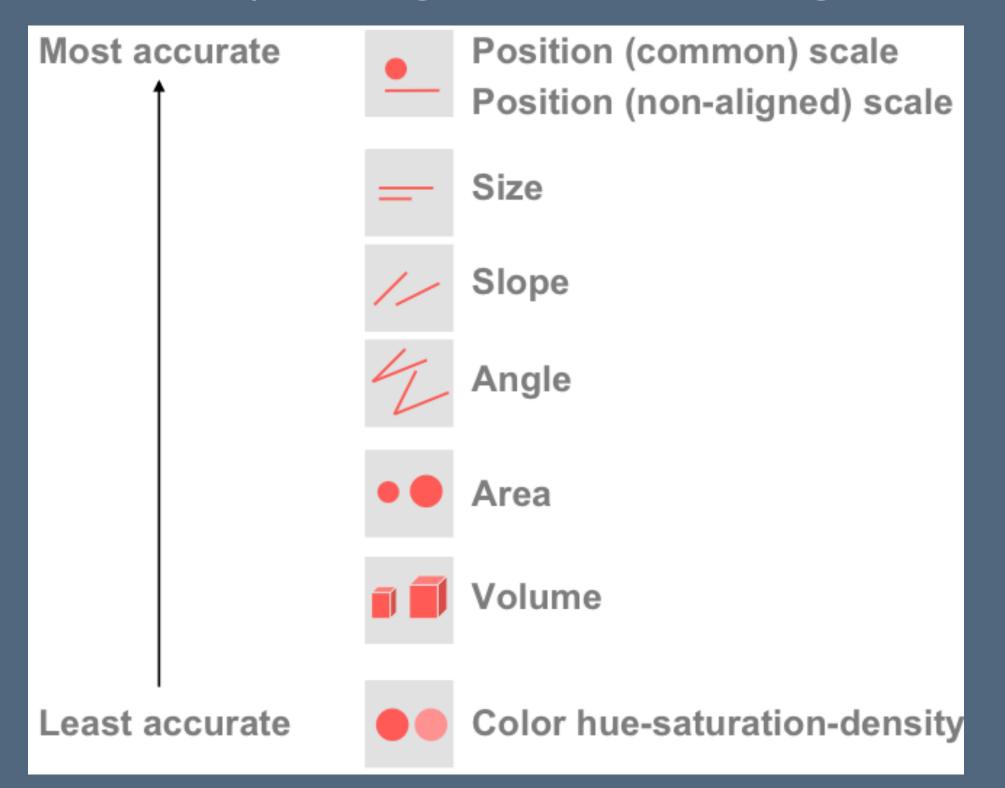


Answers — map onto each cell to the left:



Result of systematic experimentation

In comparing relative magnitude:

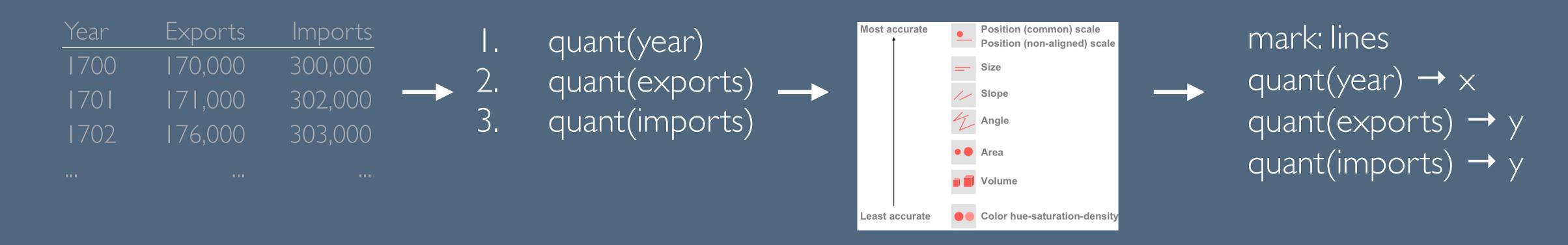


Why pie charts get hate

Graphical perception enables chart construction

[Mackinlay 1986]

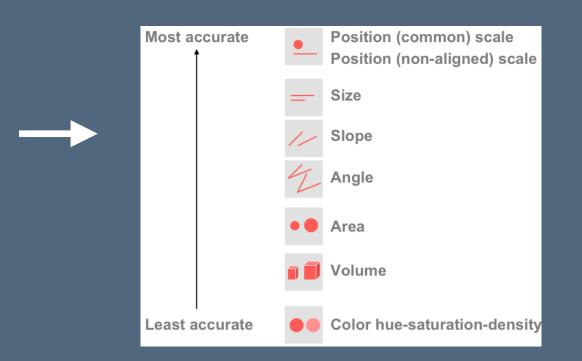
Algorithm: encode the most important data using the highest-ranking visual variable for the data type



Graphical perception enables chart construction

[Mackinlay 1986]

Algorithm: encode the most important data using the highest-ranking visual variable for the data type

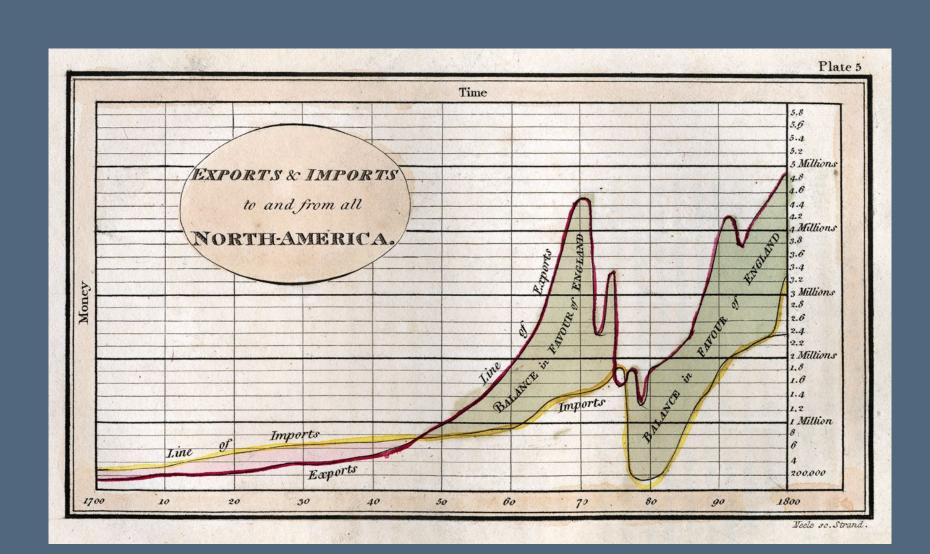


```
mark: lines

quant(year) → x

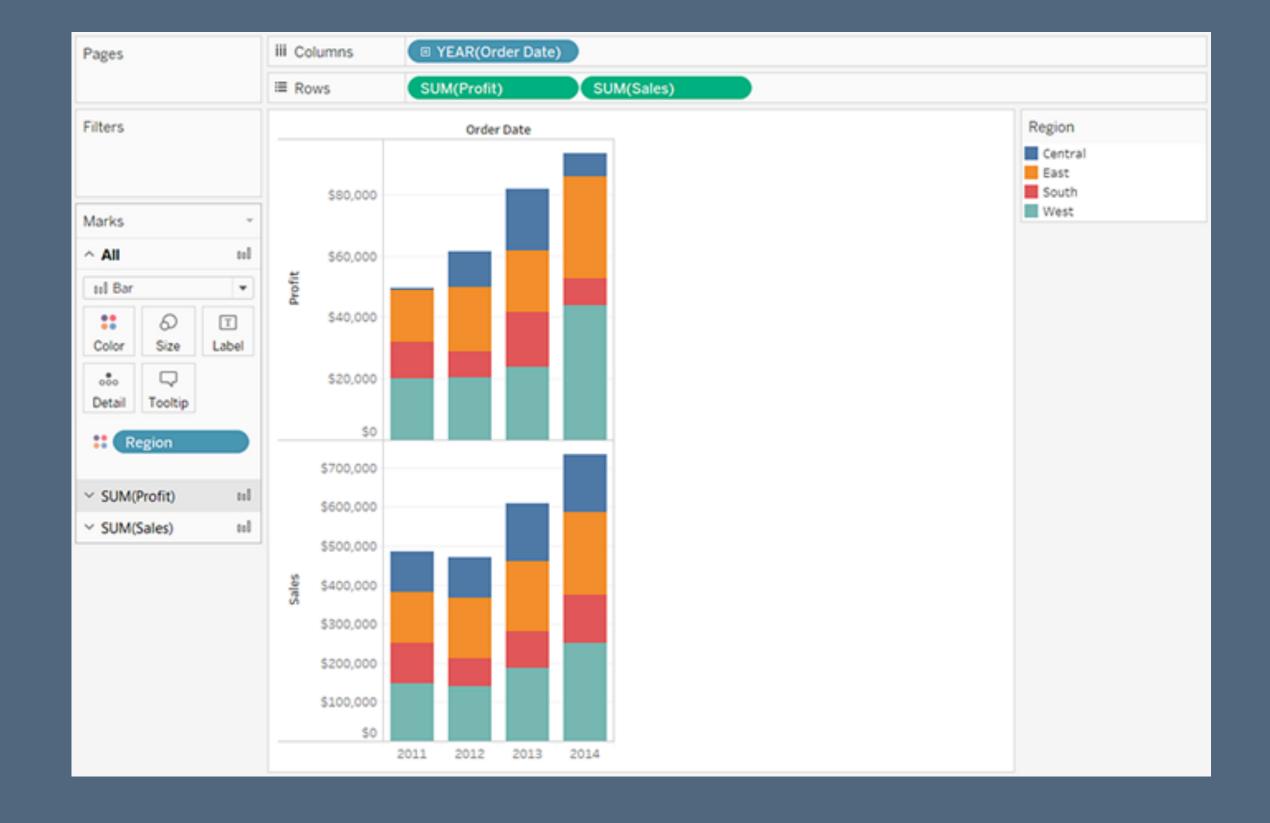
quant(exports) → y

quant(imports) → y
```



Impact

Mackinlay's algorithm gets extended by Chris Stolte and Pat Hanrahan into VizQL, which then becomes...



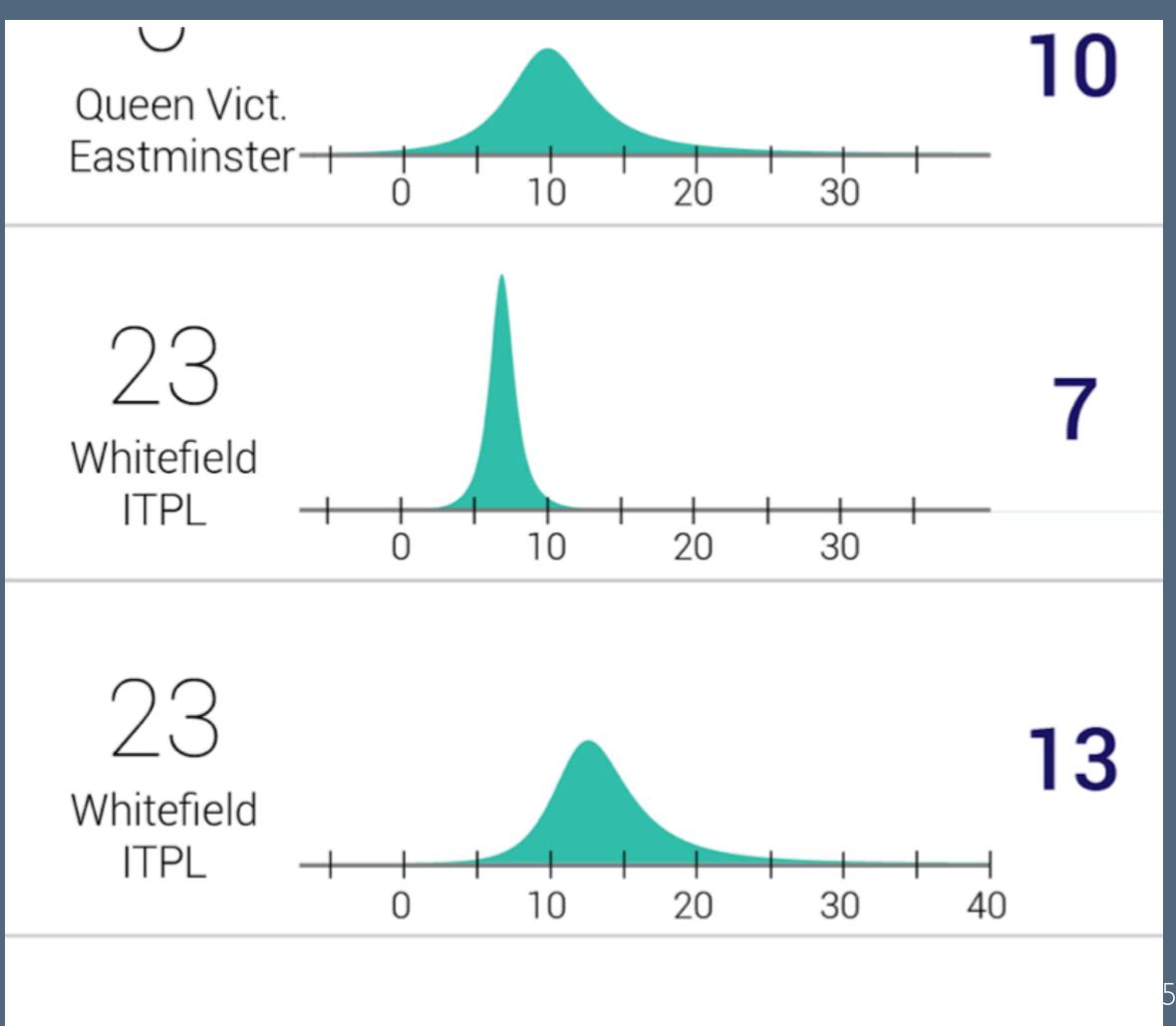


Frontiers of Visualization Research

Conveying uncertainty

[Kay et al. 2016]

We over-rely on point estimates. People simplify distributions and attend to point estimates on the right (10min until the bus comes)



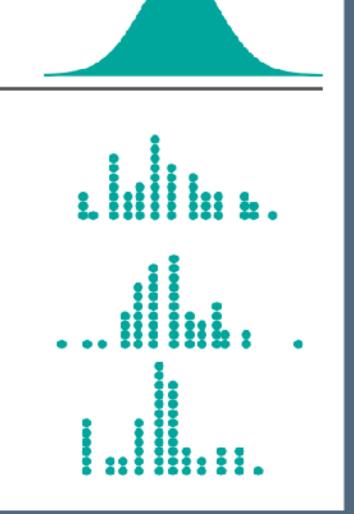
Conveying uncertainty

[Kay et al. 2016]

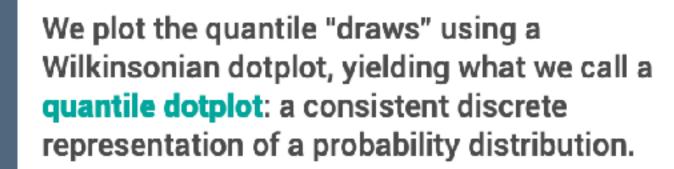
Suggestion: quantile dot plots

Probability density of Normal distribution

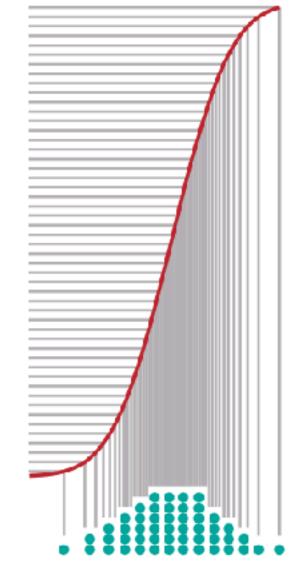
To generate a discrete plot of this distribution, we could try taking random draws from it. However, this approach is noisy: it may be very different from one instance to the next.



Instead, we use the quantile function (inverse CDF) of the distribution to generate "draws" from evenly-spaced quantiles.



By using quantiles we facilitate interval estimation from frequencies: e.g., knowing there are 50 dots here, if we are willing to miss our bus 3/50 times, we can count 3 dots from the left to get a one-sided 94% (1 - 3/50) prediction interval corresponding to that risk tolerance.

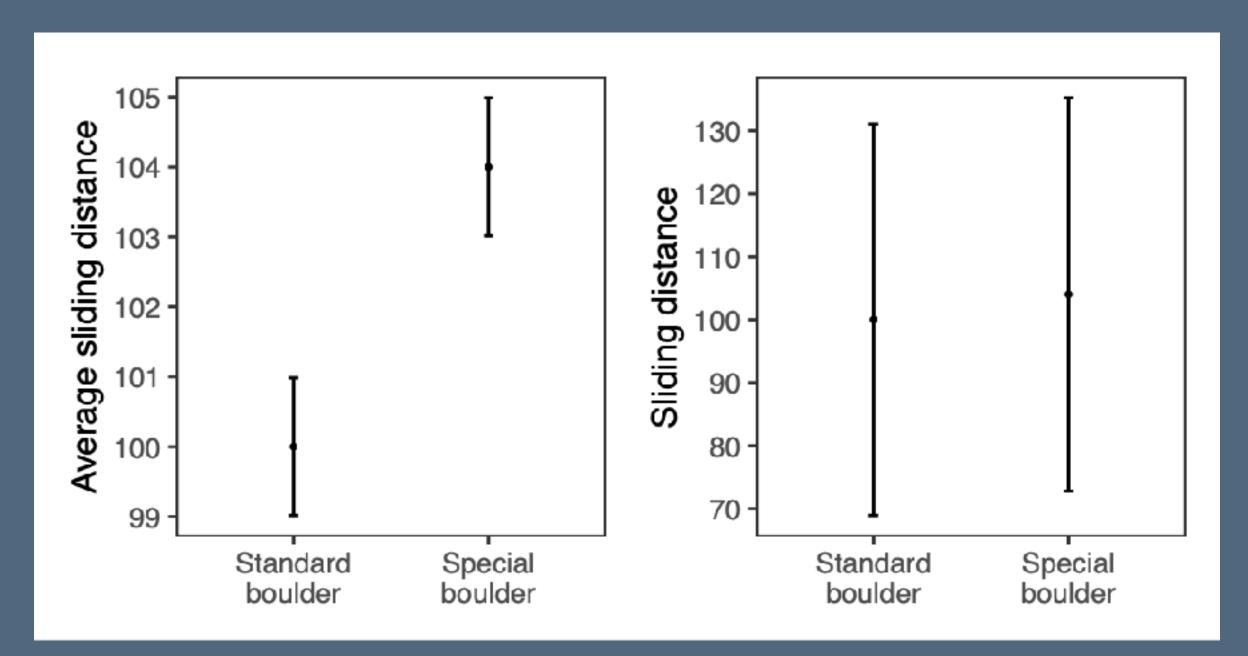




Interpretation errors

[Hofman, Goldstein, and Hullman 2020]

Two common visualizations of uncertainty:



Std. Error: uncertainty in the population mean

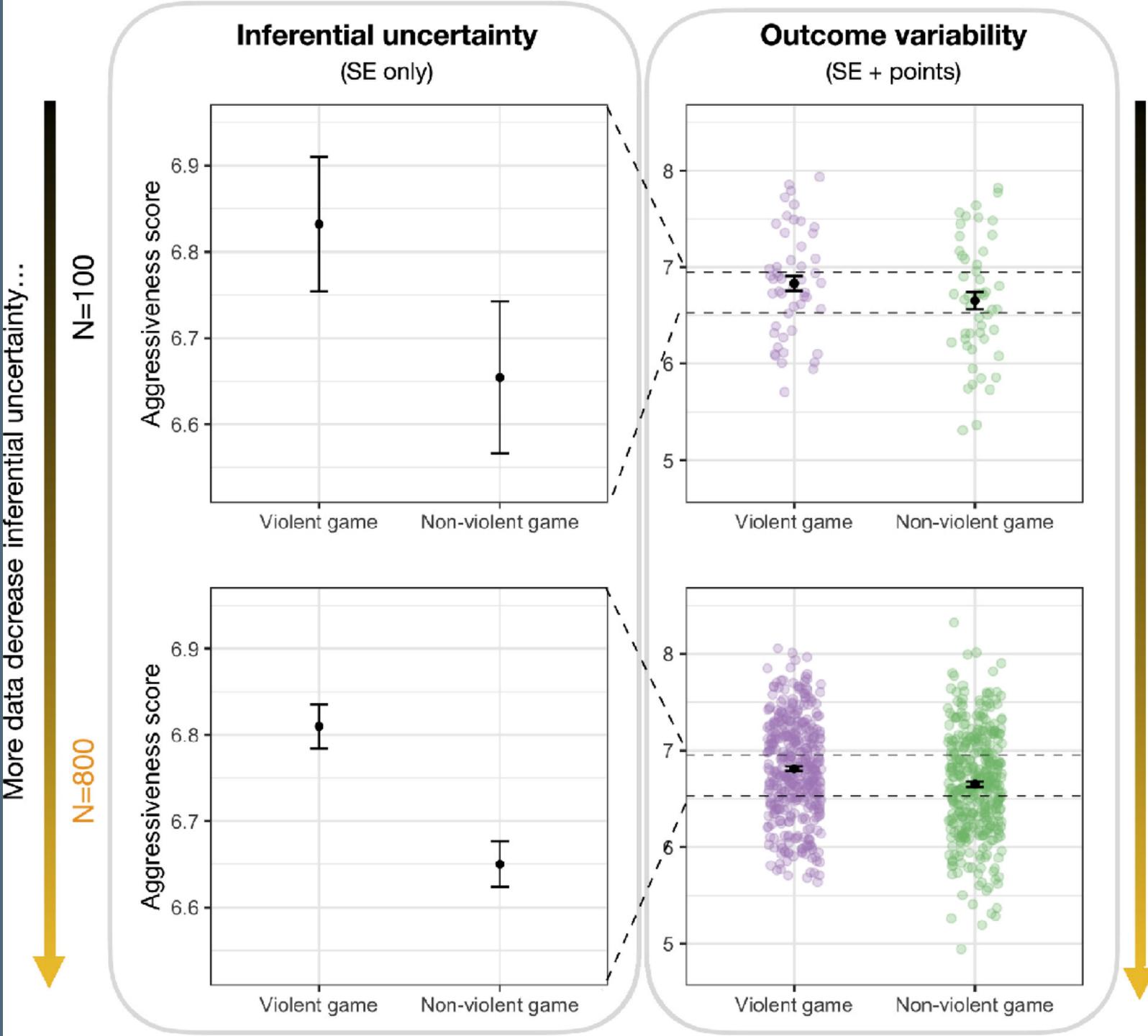
Std. Deviation: uncertainty in a single sample

Experiment: people overestimate treatment effects when shown standard errors instead of standard deviation

Uncertainty or variability?

[Zhang et al. 2023]

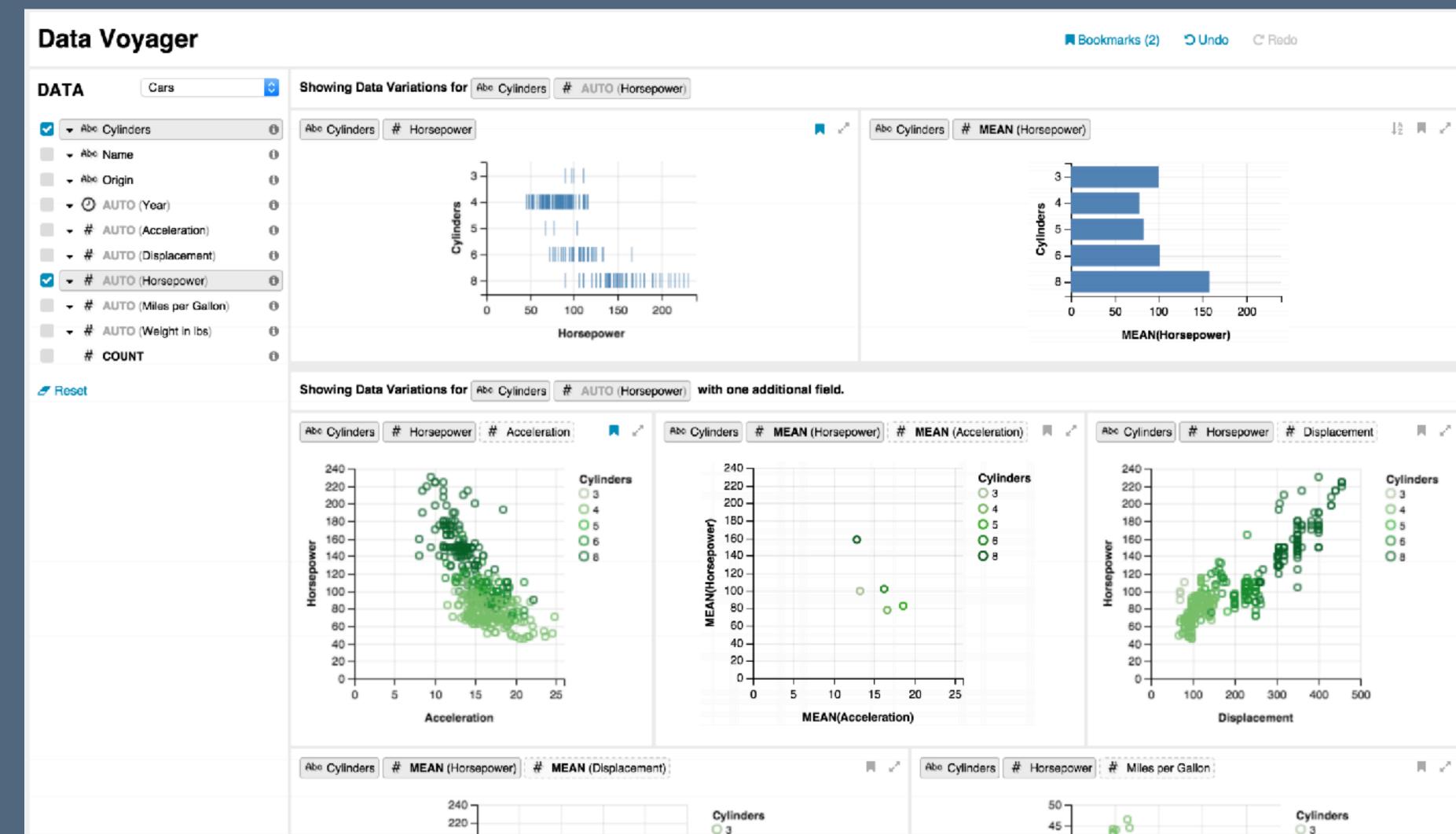
Even experts draw the wrong conclusions: "The prevalent form of visualizing only inferential uncertainty can lead to significant overestimates of treatment effects, even among highly trained experts."



Exploratory analysis

[Wongsuphasawat et al. 2015]

User inputs dataset and variables of interest, and recommender automatically generates visualizations of relevant other variables



Intentionally difficult?

[Hullman and Adar 2011]

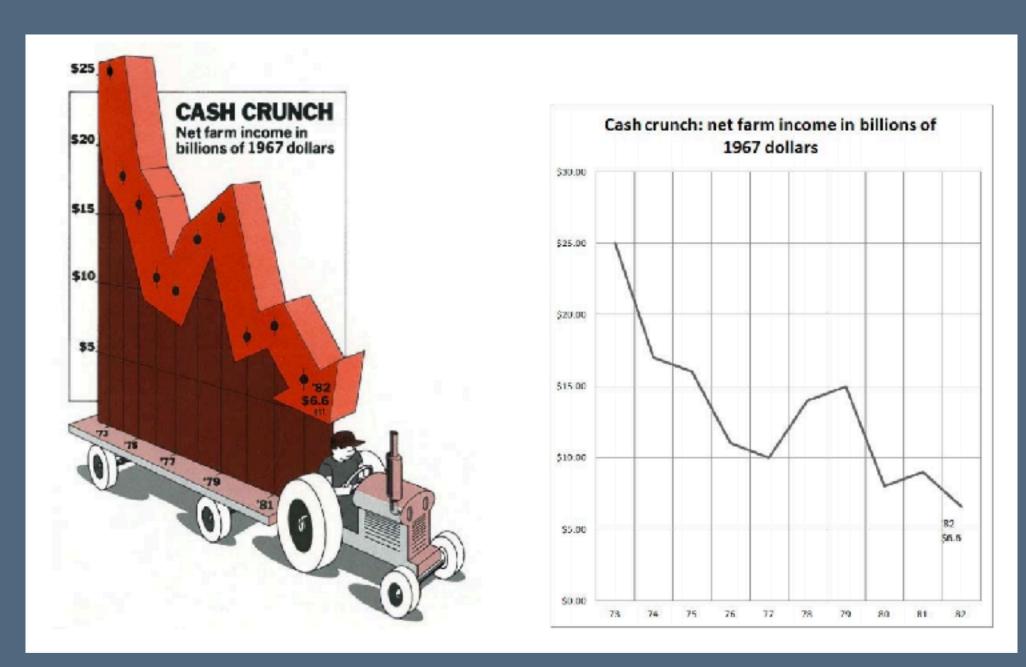
Generally, visualization (and HCl more broadly) argue optimizing for clear and correct interpretation

Yet difficult visualizations may support better comprehension and recall

Why? It induces active processing:

Forcing active construction of meaning

Disfluent learning experiences avoid heuristics and superficial reasoning



Difficult with chartjunk

Easy

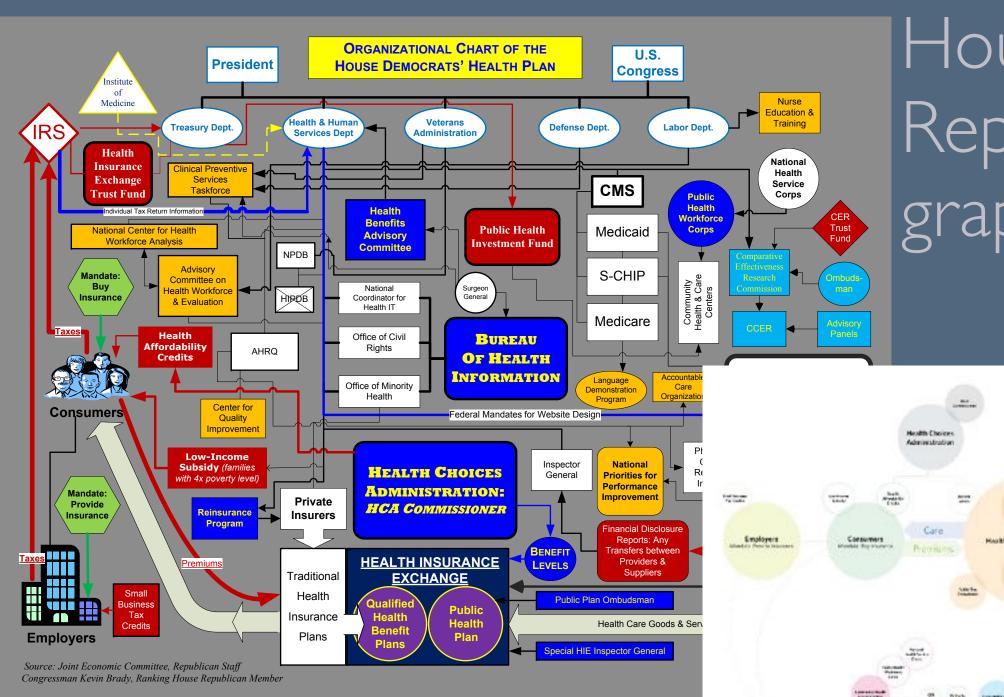
Rhetoric and visualization

[Hullman and Diakopoulos 2011]

Visualizations embed rhetorical goals to tell a story

Semiotics: signs derive their meaning from culture and other signs placed near them

Rhetoric gets embedded by omission, by how we represent uncertainty, by visual metaphor (up and right = good), and others



ers "Do not %*#& with graphic designers" response by Robert Palmer

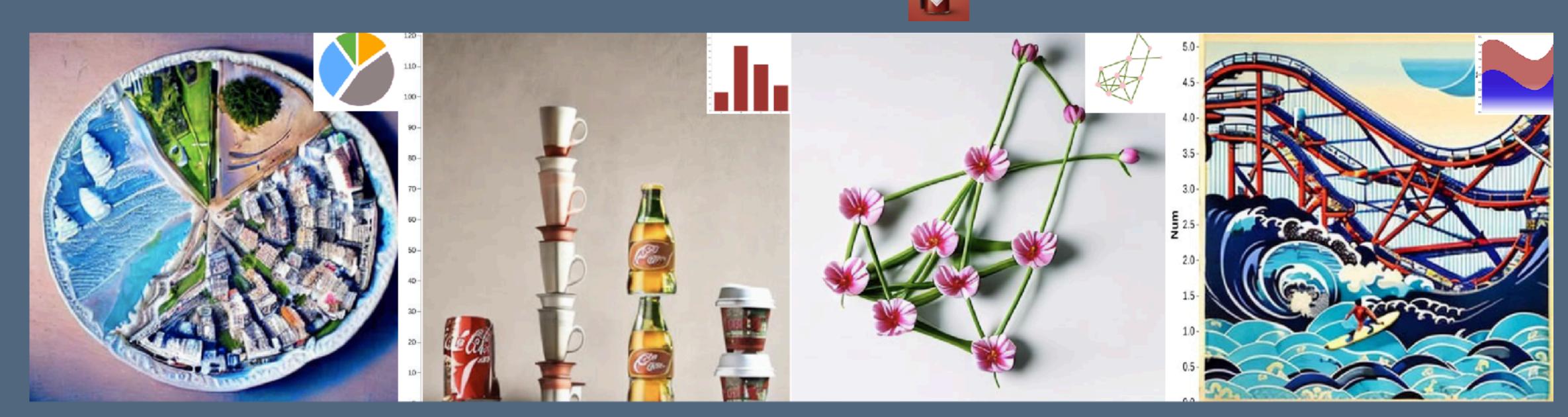
House of Representatives graphic

Conveying rhetoric visually

[Wu, Chung, and Adar 2023]

Draw on the control techniques described in the "Black Box" lecture to make visualizations that reflect some desired underlying narrative or semiotics

Remember the "visual blends" example?



S vis 'truth'? [Lee et al. 21]

Narrative visualization can be tuned to any goal: a group of scientific skeptics used the rhetorics of science and visualization to "follow the data" on COVID vaccines to its own conclusions

Visualization is not an objective process that always produces correct answers

Viral Visualizations: How Coronavirus Skeptics Use Online Data Practices to Promote Unorthodox Science Online Massachusetts Institute of Technology Cambridge, MA, USA Arvind Satyanarayan Crystal Lee arvindsatya@mit.edu Massachusetts Institute of Technology Massachusetts Institute of Technology Throughout the coronavirus pandemic, researchers have held up Cambridge, MA, USA Cambridge, MA, USA Graham M. Jones Inrougnout me coronavirus pandemic, researchers nave neid up the crisis as a "breakthrough moment" for data visualization in the crisis as a "breakthrough moment" and the crisis and the tne crisis as a preakthrough moment for data visualization fection search [91]: John Burn-Murdoch's line chart comparing infection Massachusetts Institute of Technology 1 INTRODUCTION search [91]: John burn-wurdoch s nne chart comparing mechon states across countries helped millions of people make sense of the rates across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of people make sense of the rate across countries helped millions of the rate across countries helped millions of the rate across countries across countri rates across countries neipea millions of people make sense of the United States [44], and even top Trump adpartment of the United States [44]. Cambridge, MA, USA panaemic s scale in the United States [44], and even top Trump ad ministration officials seemed to rely heavily on the Johns Hopkin. ministration officials seemed to refy neavily on the Johns Hopkir University COVID data dashboard [70]. Almost every US state no boots a data dashboard and the seed and the s hosts a data dashboard on their health department Website to she nosis a data dashboard on their nearth department website to she how the pandemic is unfolding. However, despite a preponderal of oxidence that most a second control oxidence that most a now the pandemic is uniouning. Thowever, despite a preponders of evidence that masks are crucial to reducing viral transmiss.

Controversial understandings of the coronavirus pandemic have Controversiai understandings of the coronavirus pandemic nave turned data visualizations into a battleground. Defying public health are coronavirus alreation on the coronal modic around. officials, coronavirus skeptics on US social media spent much of spent and spent much of spent much omerais, coronavirus skepues on US sociai meuia speni much visualizations showing that the government's This 2020 creating data visualizations and that the origin media and the contract of t pandemic response was excessive and that the crisis was over. This or evidence that masks are crucial to reducing viral transmit the United States have argue [25, 29, 105], protestors across the United States. panueum response was excessive and marine crisis was over. Ims

paper investigates how pandemic visualizations circulated on social local governments to overturn their mask mandates and beg paper mivesugaies now panuemic visuanzauons circulated on social the scientific estabmedia, and shows that people who mistrust the scientific and shows that people who mistrust date driven decision lightent often denless the same shotories of date driven decision. opening schools and businesses. A pandemic that affects meura, and snows that people who mistrust the scientific establishment often deploy the same rhetorics of data-driven decision.

Ishment often deploy the same rhetorics of data-driven decision. they reason, should not impinge on the liberties of a major making used by experts, but to advocate for radical policy changes. making used by experts, but to advocate for radical policy changes.

Using a quantitative analysis of how visualizations spread on the condense of the condens Using a quantitative analysis of now visualizations spread on Iwiter and an ethnographic approach to analyzing conversations at conversations and an ethnographic approach to analyzing conversations. ter and an ethnographic approach to analyzing conversations about COVID data on Facebook, We document an epistemological gap that looks are and anti-most grown to know Arostically different and the looks are and anti-most grown to head and grown that leads pro- and anti-mask groups to draw drastically defined and the description of t that leads pro- and anti-mask groups to araw arasucany unterent that leads pro- and anti-mask groups to araw arasucany unterent that the deploying argument of the following similar data. Ultimately, we argue that the deploying form the following that the deploying argument of the following that the deploying the deploying that the deploying t interences from similar data. Unimatery, we argue that the deproyment of COVID data visualizations reflect a deeper sociopolitical rift regarding the place of science in public life.

· Human-centered computing

Empirical studies in visu-• riuman-cemered computing — empirical studies in visu-concepts and paradigms; So-

book. data lit-

go about life as usual. To support their arguments, these pr go avout me as usual. To support their arguments, these parties and activists have created thousands of their own visual often using the same datasets as health officials. This paper investigates how these activist networks us of scientific rigor to oppose these public health measure ignoring scientific evidence to argue for individual fre maskers often engage deeply with public datasets and maskers onen engage deepry when Public datasers at we call "counter-visualizations"—visualizations methods to make unorthodox arguments—to challen narratives that the pandemic is urgent and ongo narrauves man members to "follow the data," these to data visualizations to support significant local cha



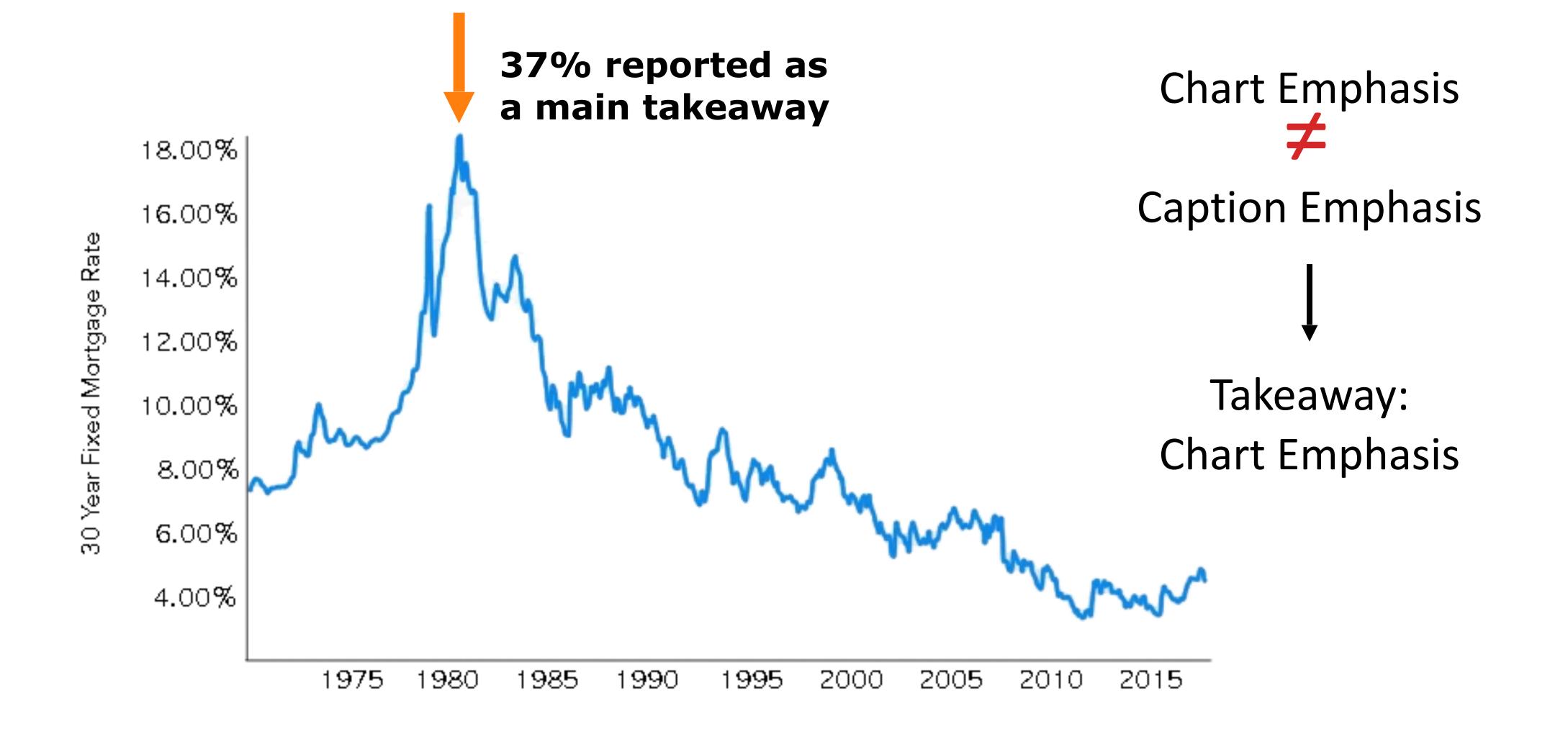




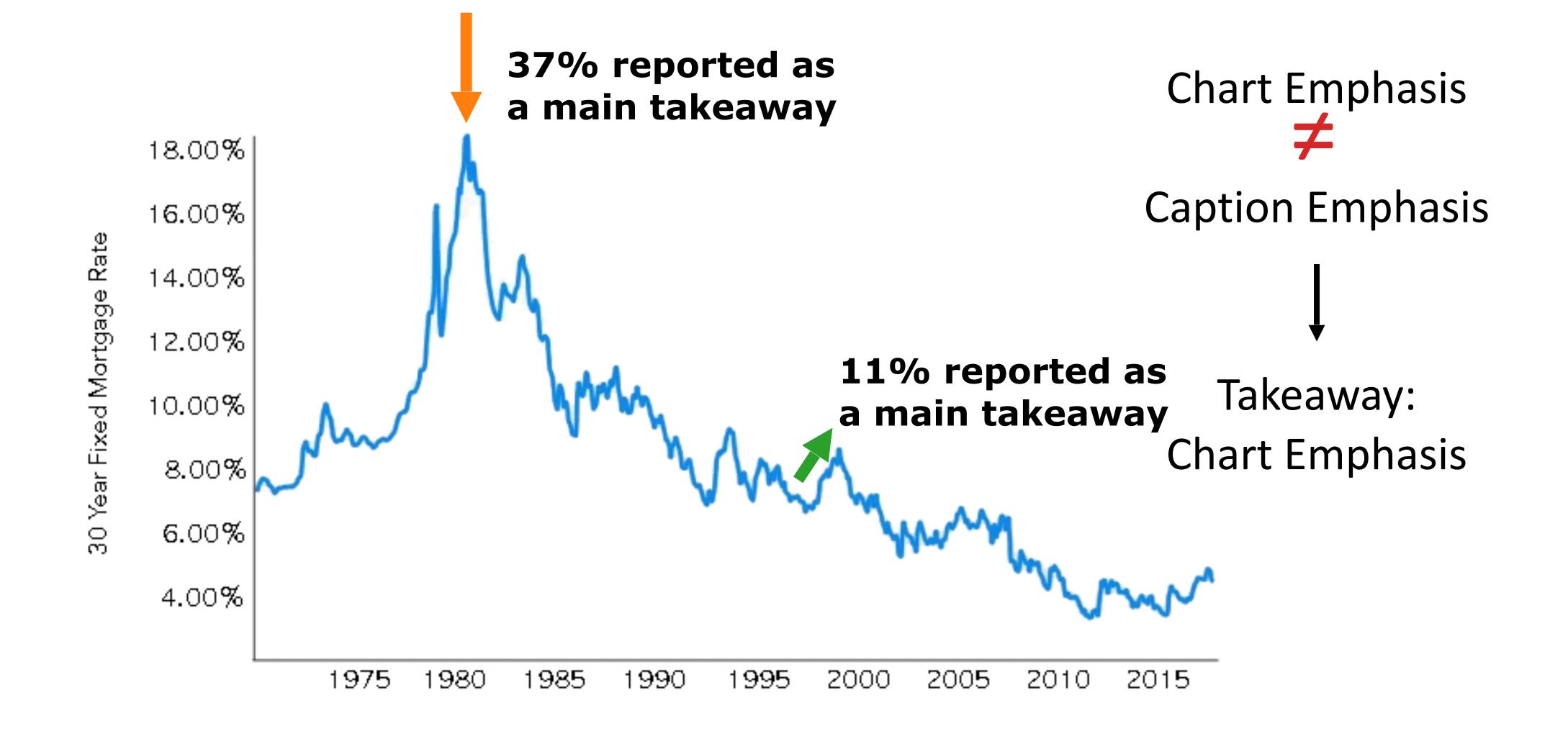
The 30-year fixed mortgage rate increased slightly from 1997 to 1999.



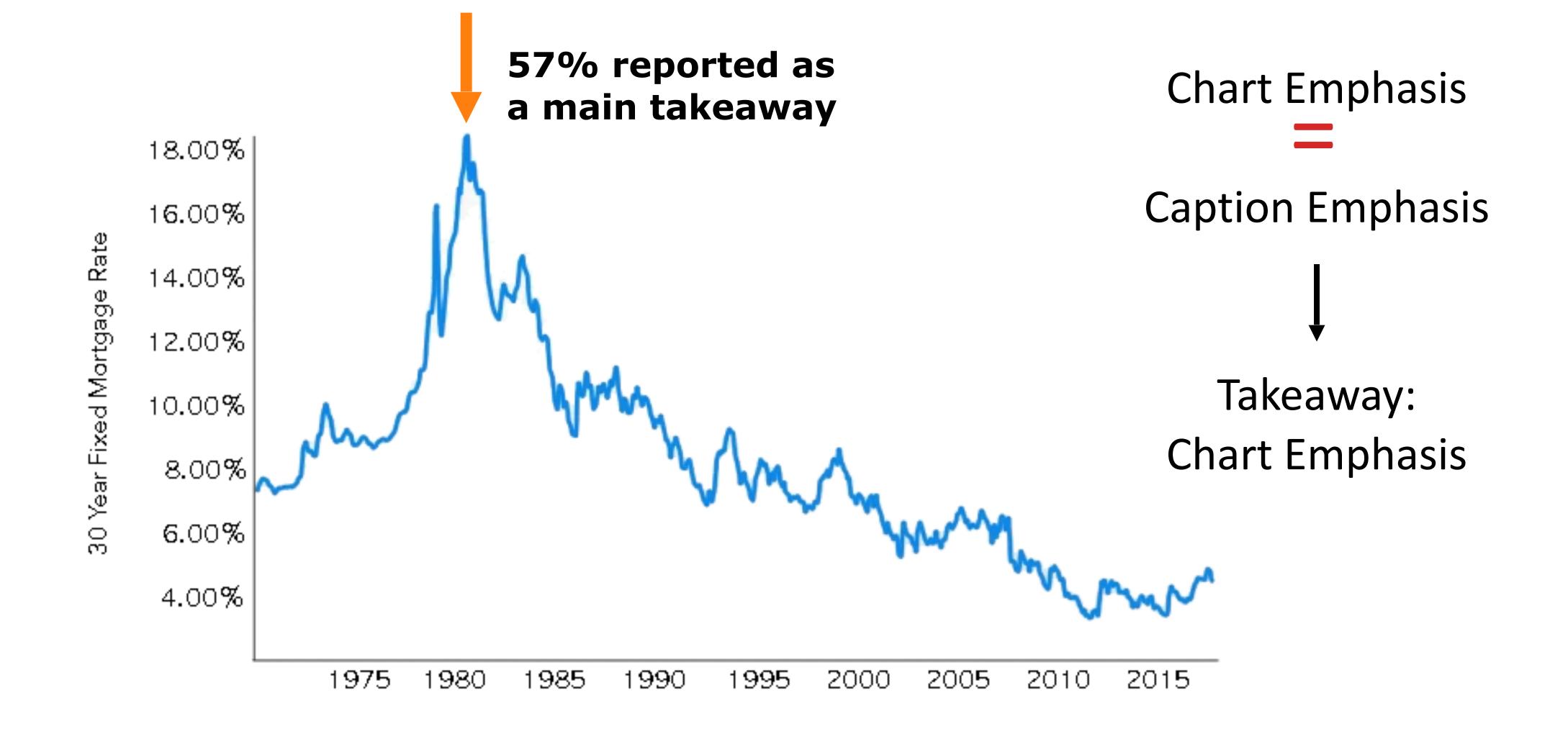
The 30-year fixed mortgage rate increased slightly from 1997 to 1999.



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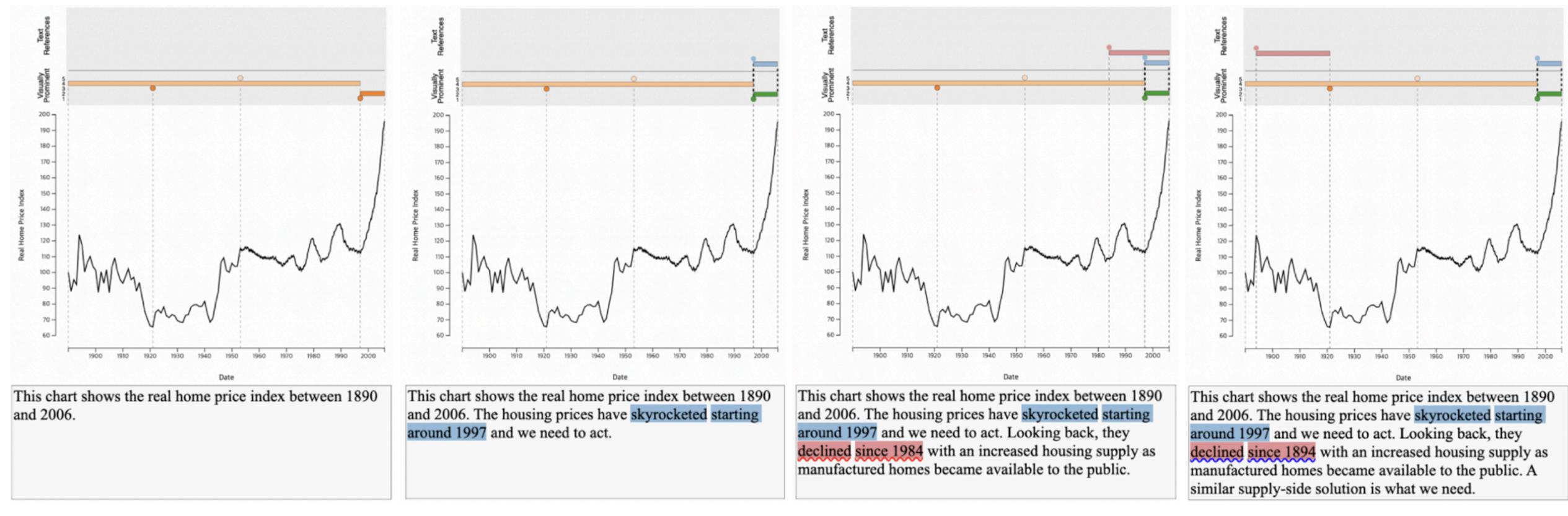


The 30-year fixed mortgage rate reached its peak of 18.5% in 1981.

Reading Charts and Captions

[Kim et al. 2021]

When text and visualization emphasis **mismatch**, readers **rely more on the chart** and can miss information in the caption.



(a) Prominent features & Basic caption

(b) Caption text about prominent feature

(c) Caption including false information

(d) Caption about less prominent feature

Summary

Visualizations can be represented as **encodings** that map from **data to marks & visual attributes** based on **data types**

Our cognitive and perceptual systems determine which encodings are effective: we (mis)read data if encoded poorly

Active research at frontiers investigating how users can create effective visualizations and how readers take information away from them

CS 448B Visualization

Stanford CS course on data visualization techniques (Fall 2021)

Location: Huang Eng. 18 Time: MW 11:30am-1pm

ABOUT

LEARNING GOALS

TEXTBOOKS/RESOURCES

SCHEDULE

Week 1

Week 2

Week 3 Week 4

Week 5

Week 6

Week 7

Week 8

Week 9

Week 10

TEACHING STAFF

ASSIGNMENTS

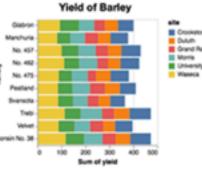
Class Participation

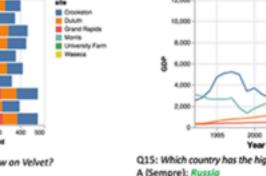
Assignment 1

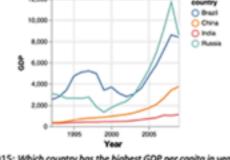
Assignment 2

Assignment 3 Final Project

How Common Is Religious Extremism? Q1: What is the percentage of response A(Ours): 8. I looked up the length of the Pagan/earth-based orange bar for 'Catholics'. Q2: Which religion has the longest orange Unaffiliated A(Sempre): Hindus AlOurs); Muslims, I looked up 'Religion' o the longest orange bar. Orthodox Christian Q3: What does the blue field represent? Buddhists







A (Ours): 87.633, I looked up the length of the yellow bar for 'Velver', A (Ours): Russia, I looked up 'country' of the highest line for '2005'. Q16: How many times do Brazil and Russia flip in terms of GDP ranking A (Ours): Trebi. I looked up 'variety' of the longest blue bar. A (Ours): 2. I counted the number of the blue line or the cyan line.

Well designed visualizations capitalize on human facilities for processing visual information and thereby improve comprehension, memory, inference, and decision making. In this course we will study techniques and algorithms for creating effective visualizations based on principles from graphic design, visual art, perceptual psychology and cognitive science. The course is targeted both towards students interested in using visualization in their own work, as well as students interested in building better visualization tools and systems.

represents by looking at the legend.

There are no official prerequisites for the class, but familiarity with the material in CS147, CS148 and CS142 is especially useful. Most important is a basic working knowledge of, or willingness to learn, web-programming, especially JavaScript, Vega-Lite and D3.js. While we will cover a little bit of Vega-Lite and D3.js in class, we will also expect students learn some introductory material, especially about Javscript on their own, as necessary. Tutorials on Javascript are available on the web and we will help you find the relevant information as you need it.

*Contact us via Slack if you are worried about whether you have the background for the course.

Learning Goals

The goals of this course are to provide students with the foundations necessary for understanding and extending the current state of the art in visualization. By the end of the course, students will have:

- An understanding of key visualization techniques and theory, including data models, graphical perception and methods for visual encoding and interaction.
- Exposure to a number of common data domains and corresponding analysis tasks, including exploratory data analysis and network analysis.
- Practical experience building and evaluating visualization systems using Vega-Lite and D3.js.
- The ability to read and discuss research papers from the visualization literature.

Textbooks/Resources

- 1. The Visual Display of Quantitative Information (2nd Edition). E. Tufte. Graphics Press.
- Envisioning Information. E. Tufte. Graphics Press.
- 3. Optional Textbook. Visualization Analysis and Design. Tamara Munzner. A K Peters Visualization Series, CRC Press.
- 4. Optional Reference. Interactive Data Visualization for the Web (2nd Edition). Scott Murray. O'Reilly Press. [Read Online] [Code Examples on Github]

Your best bet is to order them online. Please order soon. Readings will be assigned in the first week of class.

To learn more about visualization consider taking CS 448B: Fall 2025

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- Practical experience building and evaluating visualization systems using Vega-Lite and D3.js.
- The ability to read and discuss research papers from the visualization literature.

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